

Coupled root water and solute uptake – a functional structural model

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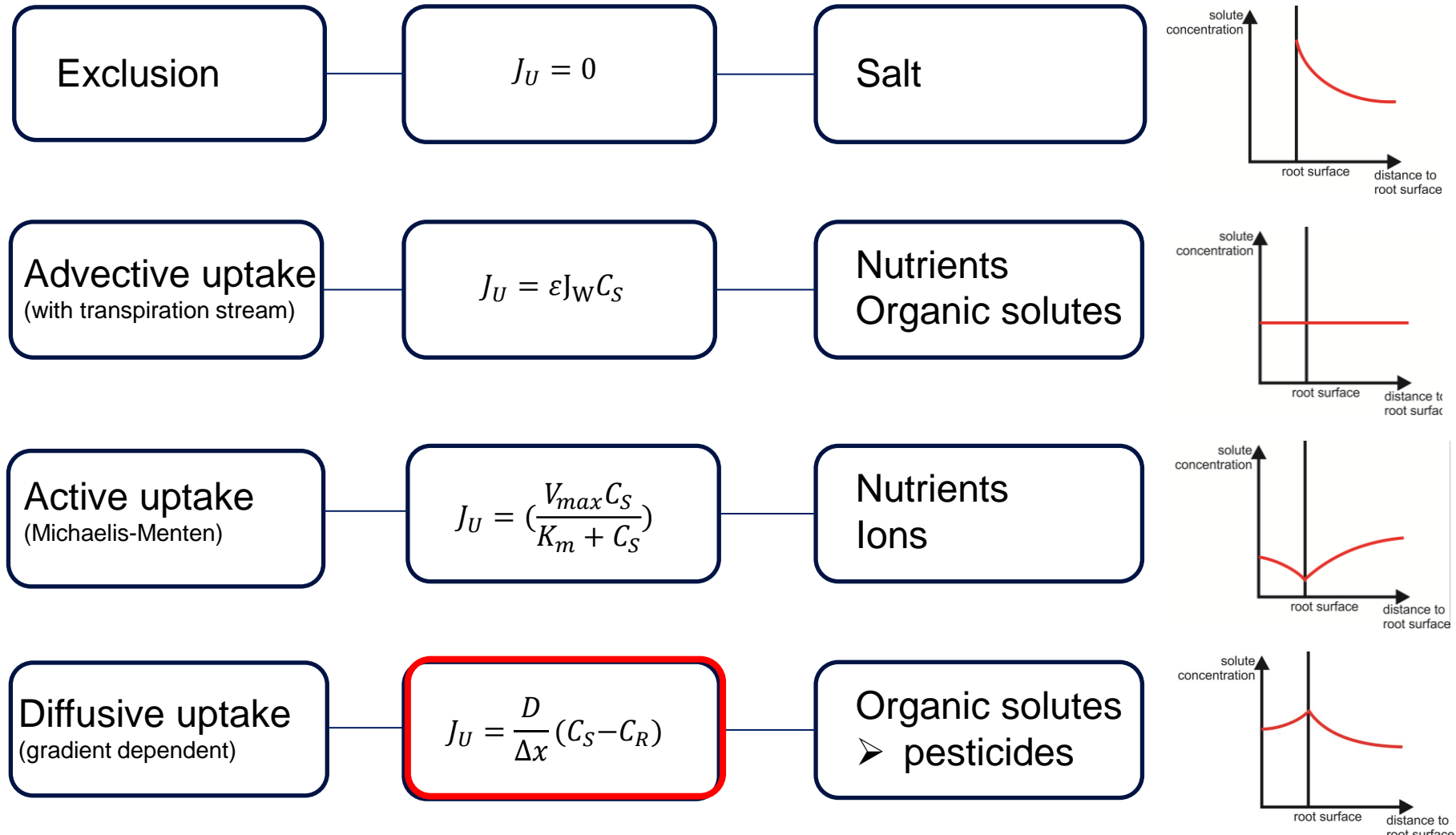
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6 September, 2017

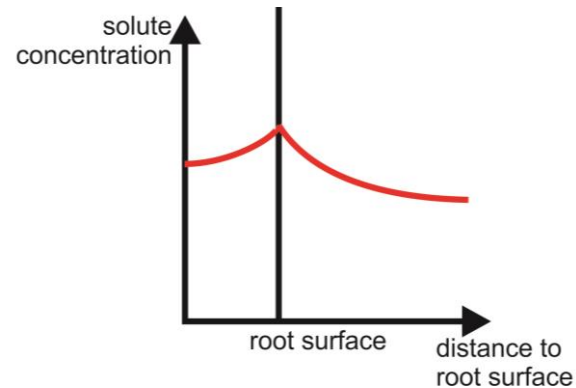
Motivation 1

Root solute uptake mechanisms:



Motivation 1

Diffusive uptake



Challenge:

Simulate solute uptake of roots considering

- soil solute and root concentration
- with interaction and feedback between soil and root system.

Motivation 2

EU model for pesticide legislation

$$J_U = J_W * f * C_S \quad [M \ T^{-1} \ L^{-2}]$$

Uptake factor f:

$$TSCF = \frac{C_X}{C_S} \in [0,1][-]$$

≠

$$PUF = \frac{C_{upt}}{C_S} \in [0,1][-]$$

- C_X : Solute concentration in plant shoot $[M \ L^{-3}]$
- C_S : Solute concentration in soil water $[M \ L^{-3}]$
- J_W : Root water flux $[L \ T^{-1}]$
- $C_{upt} = \frac{m_{upt}}{V_{upt}} \quad [M \ L^{-3}]$
- Experimentally determined with hydroponics
- Cumulative solute uptake

TSCF: Transpiration Stream Concentration Factor

PUF: Plant Uptake Factor

i.a. PEARL, Tiktak et al. 2015

Motivation 2

EU model for pesticide legislation

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Is a constant factor sufficient to represent solute uptake processes?

- Solute characteristics
- Time dependency
- Root structure
- Application procedure
- Soil characteristics

Challenge: Gain an understanding of the dynamics and dependencies of root solute uptake and their representation by TSCF and PUF

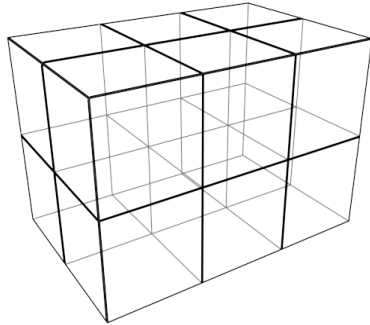
Methods

Soil and root water flow and uptake

Soil

$$\frac{\partial \theta}{\partial t} = \nabla \cdot [\mathbf{K}(\theta) \nabla (h+z)] - S(x, y, z, t)$$

Richards 1931

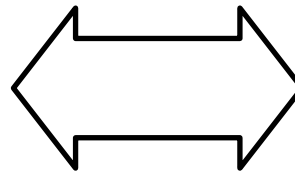


Plant Root

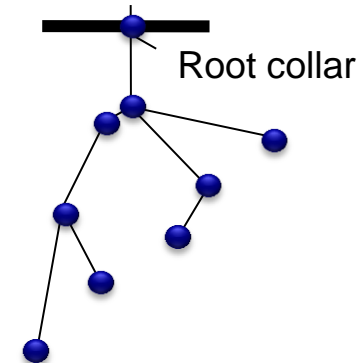
$$J_x = K_x^* A_x \frac{dH_x(z)}{dl}$$

$$J_R = K_R^* S_R [H_S(z) - H_X(z)]$$

Doussan et al. 2006



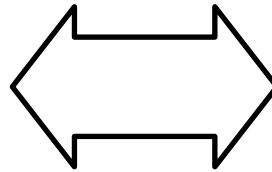
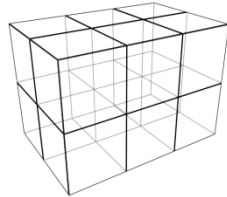
$$S = \frac{\sum_{i=1}^n J_{R,i}}{V_s}$$



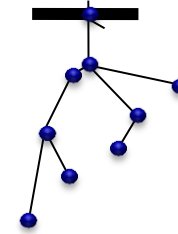
Javaux et al. 2008

Soil and root solute transport and uptake

Soil



Plant Root

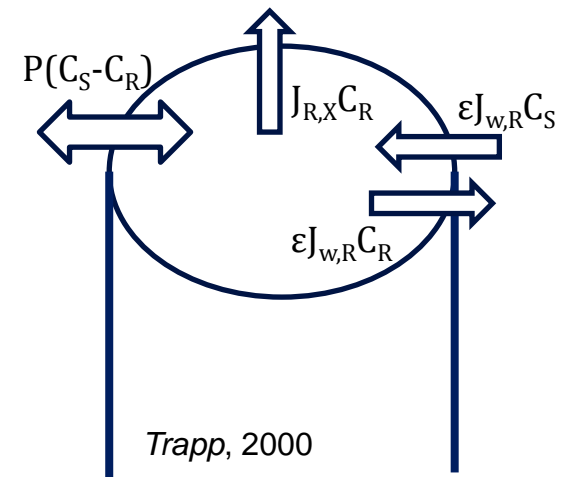


$$\frac{\partial(\theta_S + \rho_S K_{D,S})C_S}{\partial t} = \nabla \cdot (D\tau\theta_S \nabla C_S - \mathbf{J}_w C_S) - (\theta_S + \rho_S K_{D,S})k_S C_S + S_S$$

$$\frac{\partial C_R}{\partial t} = \nabla \cdot (-\mathbf{J}_{w,R} C_R) - (\theta_R + \rho_R K_{D,R})k_R C_R + S_R$$

$$S_R = \frac{A_R}{V_R} (P(C_S - C_R) + \epsilon J_{w,R} C_S)$$

$$S_S = -\frac{\sum_{i=1}^n A_{R,i} (P(C_S - C_{R,i}) + \epsilon J_{w,i} C_S)}{V_S}$$

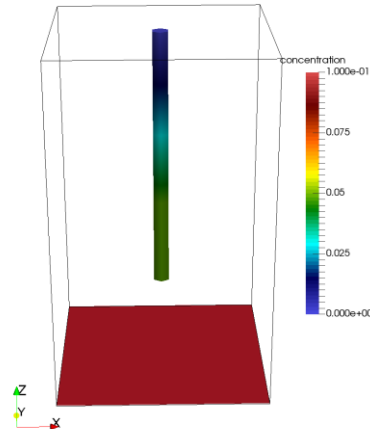


PARTRACE

Bechtold et al., 2011

Schröder et al., 2012

Benchmark scenario



Soil:

domain: $0.6 \times 0.6 \times 1 \text{ cm}^3$

$c_{S,ini} = 0.1 \text{ mg cm}^{-3}$

$Prec = 0.067 \text{ cm}^3 \text{ d}^{-1}$

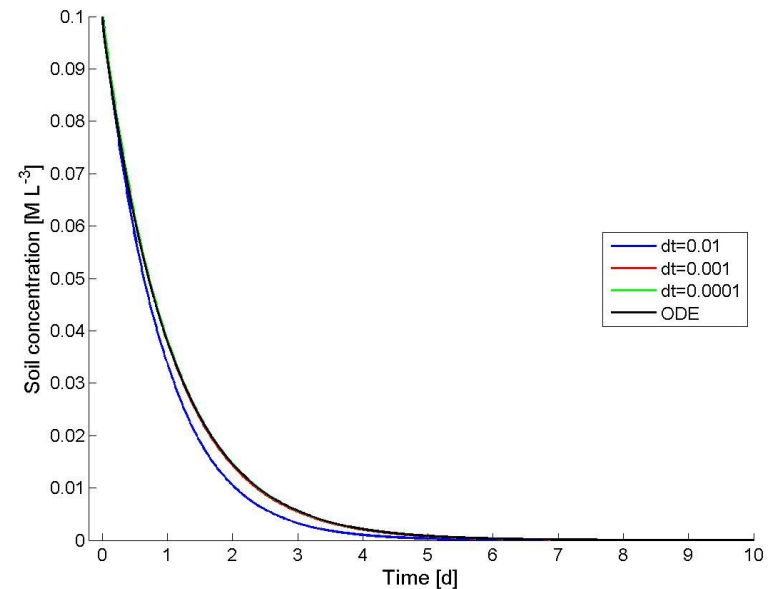
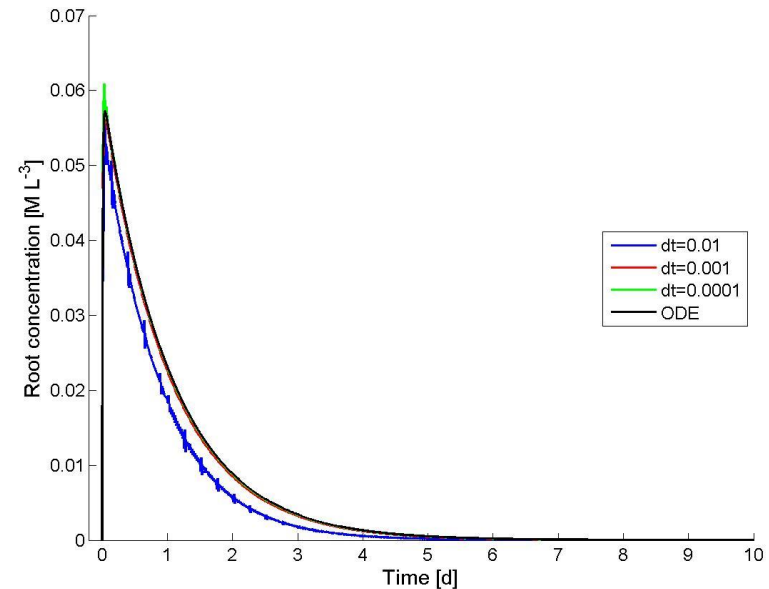
Root:

$l = 0.75 \text{ cm}$

$P = 0.864 \text{ cm d}^{-1}$

$T_{pot} = 0.067 \text{ cm}^3 \text{ d}^{-1}$

$C_{R,ini} = 0 \text{ mg d}^{-1}$



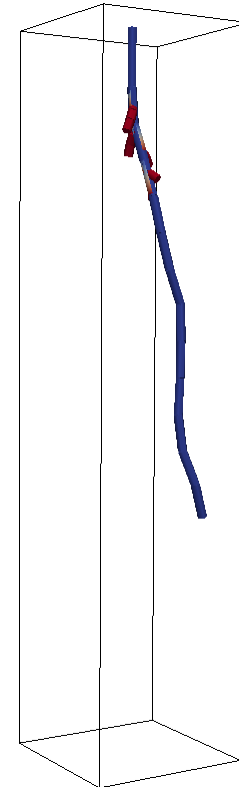
Sensitivity analysis

Soil:

- No flux boundaries
- No soil sorption
- $C_{S,ini} = 1 \text{ mg cm}^{-3}$ at $t=0$
- domain: $2.25 * 2.25 * 10 \text{ cm}^3$
with $\Delta x = \Delta y = \Delta z = 0.25 \text{ cm}$

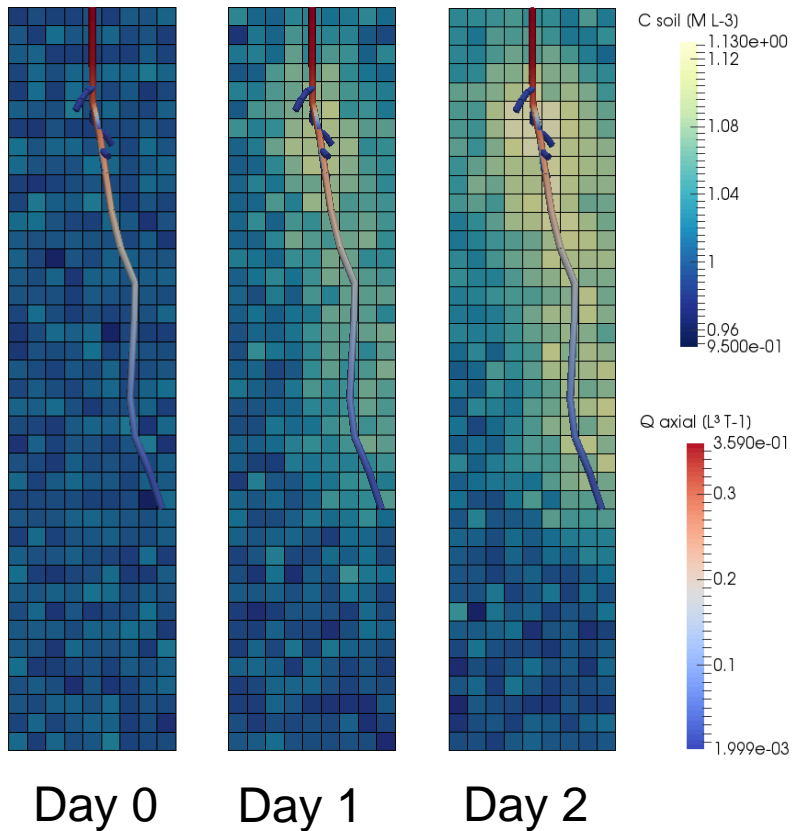
Root:

- Static root system (age 2 days)
- $T_{pot} = 0.359 \text{ cm}^3 \text{ day}^{-1}$
- $P = 5.62 * 10^{-2} \text{ cm day}^{-1}$ (low permeability)
- No sorption in root system
- $C_{R,ini} = 0 \text{ mg cm}^{-3}$ at $t=0$
- 2 days simulation time



Parametrization and results

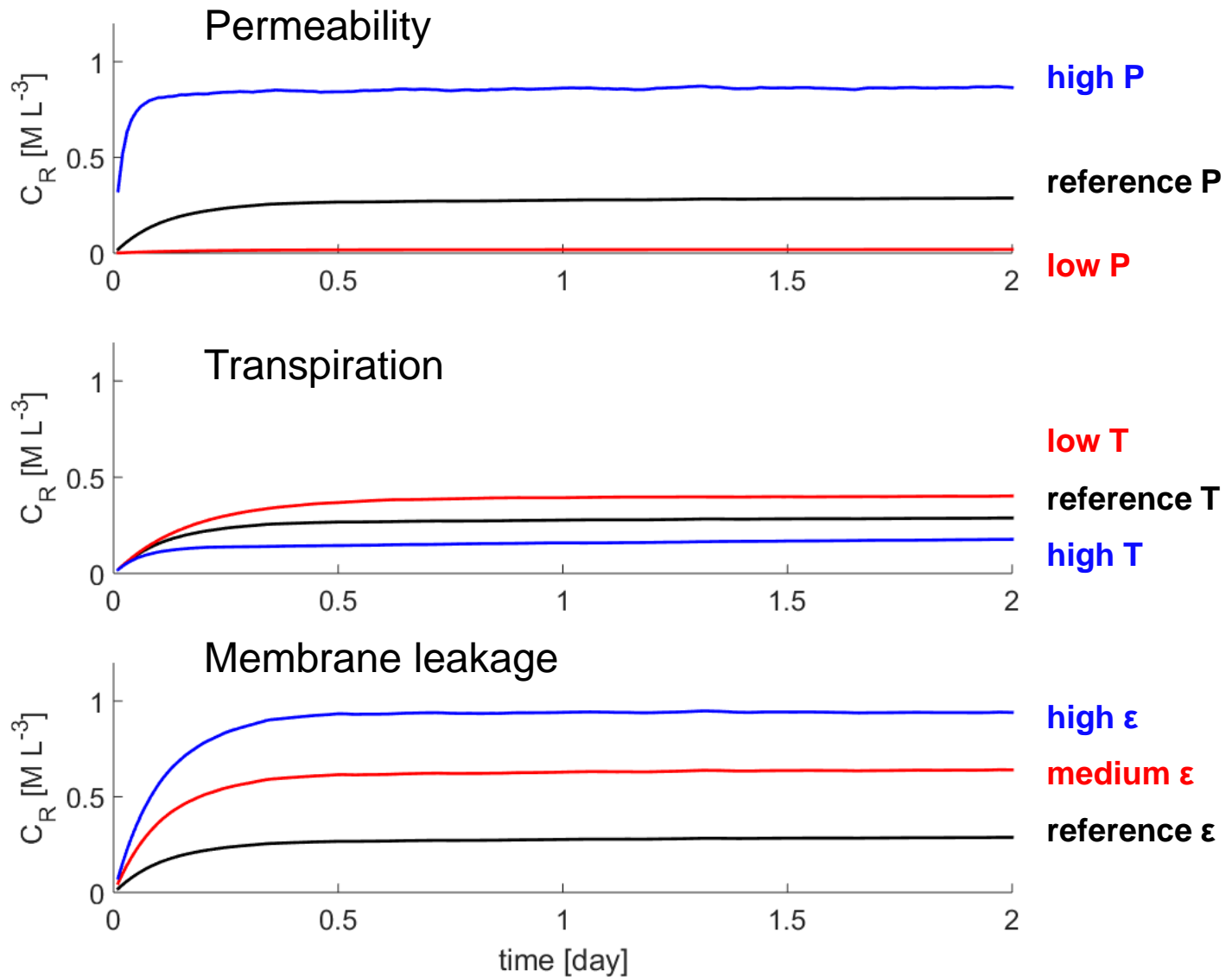
reference case



	P [cm day ⁻¹]	ε [-]	T_{pot} [cm ³ day ⁻¹]
1	5.62e-2	0.0	0.359
2	“	“	0.019
3	“	“	0.868
4	“	0.5	0.359
5	“	1.0	“
6	2.69e-3	0.0	“
7	1.18	“	“

reference

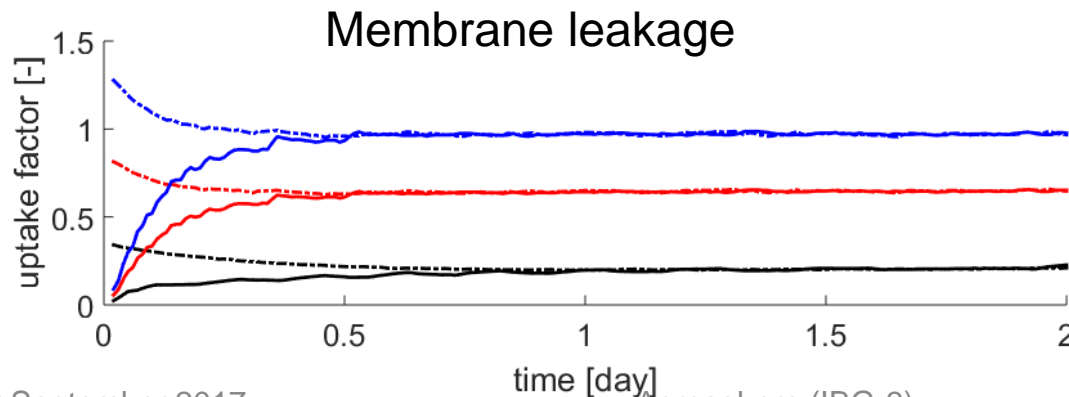
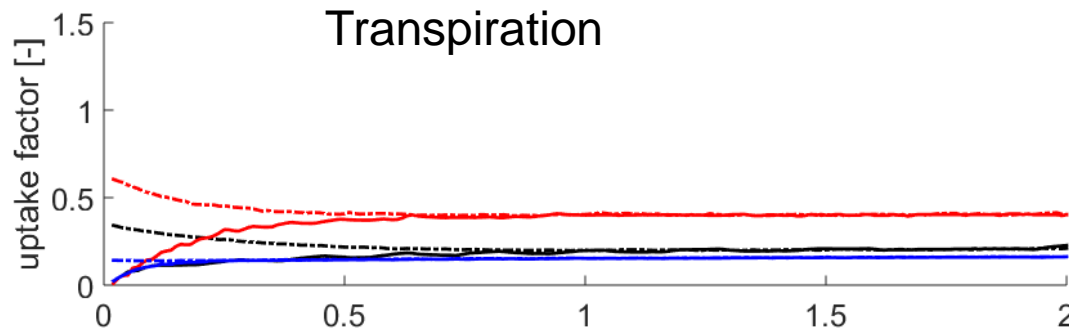
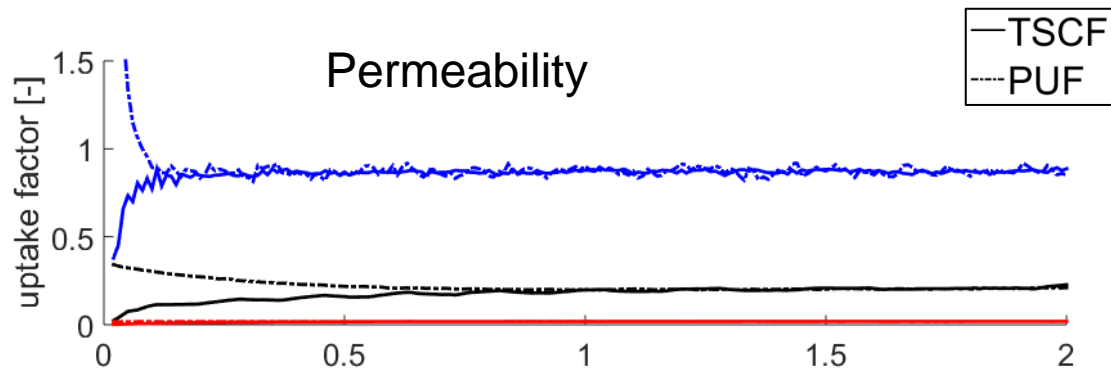
Results: root concentration



Results: uptake factors

$$PUF(t_i) = \frac{\sum_1^j m_{upt,i,j} / V_{upt,i}}{\bar{C}_S(t_i)}$$

$$TSCF(t_i) = \frac{\bar{C}_X(t_i)}{\bar{C}_S(t_i)}$$



Conclusion

- We implemented diffusive solute uptake as suggested by e.g. Trapp (2000) in a 3D multidimensional and dynamic root – soil model
- We are able to identify sensitive parameters (membrane permeability, transpiration, leakage factor) which influence the uptake and concentration of pesticides in root and soil
- We can relate the plant uptake factors to the transpiration rate and the root properties
- For the small system considered the uptake factors both reached a constant value
- Further studies with longer runtime, larger domains, more complex root systems, and more realistic boundary conditions will give a better indication how uptake factors vary in time and space or if a constant factor might be sufficient

Concentration gradients around the roots - 1D radially symmetric model

$$(\theta_R + \rho_R K_{D,R}) \frac{\partial C_{R,f}}{\partial t} = \frac{A_R}{V_R} [P(C_{S,f} - C_{R,f}) + \varepsilon J_W C_{S,f}] - \frac{Q_x}{V_R} C_{R,f} - k_R \theta_R C_{R,f}$$

$$(\theta_S + \rho_S K_{D,S}) \frac{\partial C_{S,f}}{\partial t} = \frac{1}{r} \frac{\partial}{\partial r} \left(r D \tau \theta_S \frac{\partial C_{S,f}}{\partial r} \right) + \frac{r_0}{r} J_W \frac{\partial C_{S,f}}{\partial r} - k_S \theta_S C_{S,f}$$

boundary conditions

$$D \tau \theta_S \frac{\partial C_{S,f}}{\partial r} + J_W C_{S,f} = P(C_{S,f} - C_{R,f}) + \varepsilon J_W C_{S,f}$$

$$\frac{\partial C_{S,f}}{\partial r} + \frac{r_0 J_W}{r D \tau \theta_S} C_{S,f} = 0$$

initial conditions at $t=t_0$

$$C_{R,f} = 0$$

$$C_{S,f} = C_{S,0,f}$$



Model setup

Soil:

- $\theta_S = 0.3 \text{ cm}^3 \text{ cm}^{-3}$
- $D = 6.5\text{E-}6 \text{ cm}^2 \text{ s}^{-1}$
- $C_{S,0,f} = 1\text{E-}6 \text{ g cm}^{-3}$

- Uptake by diffusion and advection: $\varepsilon = 0.05$
- BC root-soil interface: flux
- BC at $r=r1$: no flux
- 10 days of simulation

Root flow:

- $Q_X(\text{low}) = 1.27\text{E-}8 \text{ cm}^3\text{s}^{-1}$
- $Q_X(\text{med}) = 1.26\text{E-}7 \text{ cm}^3\text{s}^{-1}$
- $Q_X(\text{high}) = 5.67\text{E-}6 \text{ cm}^3\text{s}^{-1}$

Solutes

- compound 1

$$\log K_{OW} = 0.8$$

$$P_M = 1.64\text{E-}6 \text{ cm s}^{-1} \quad [\text{Lichtner and Cronshaw, 1986}]$$

$$K_{D,S} = 5.6\text{E-}2 \text{ cm}^3 \text{ g}^{-1}$$

$$K_{D,R} = 5.03 \text{ cm}^3 \text{ g}^{-1} \quad [\text{Trapp, 2000}]$$

- compound 2

$$\log K_{OW} = 2.8$$

$$P_M = 7.48\text{E-}6 \text{ cm s}^{-1}$$

$$K_{D,S} = 2.33 \text{ cm}^3 \text{ g}^{-1}$$

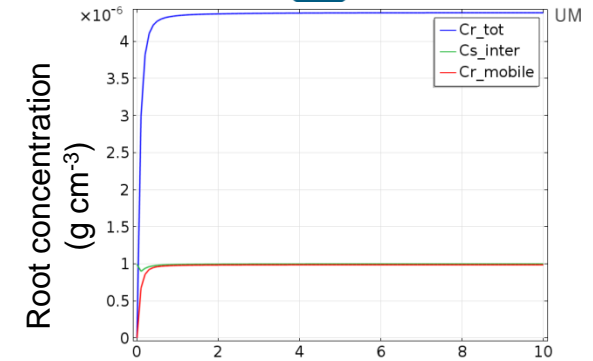
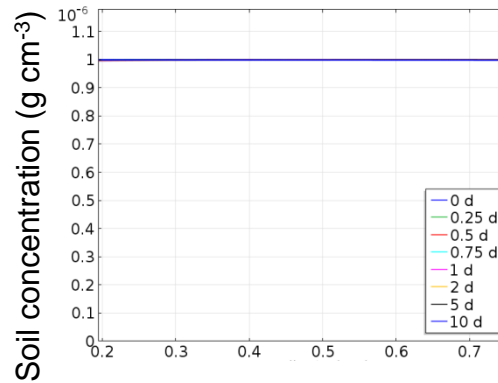
$$K_{D,R} = 174.73 \text{ cm}^3 \text{ g}^{-1}$$

Results

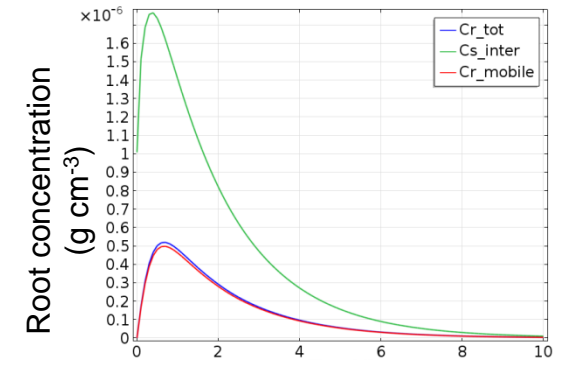
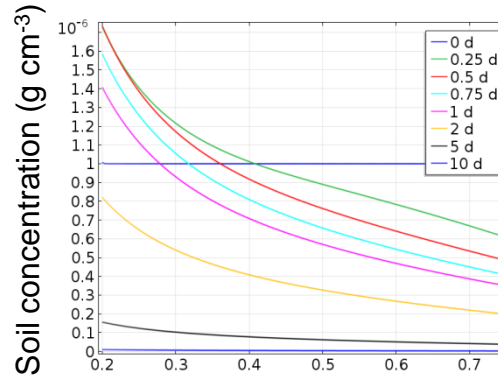
Case	Compound	water uptake
1	2 (high $\log K_{OW}$)	small
2	1 (low $\log K_{OW}$)	high
3	2 (high $\log K_{OW}$)	med

Case	Root solute uptake vs. soil solute transport	Solute sorption in roots
1	uptake \approx transport	large
2	uptake < transport	small
3	uptake > transport	large

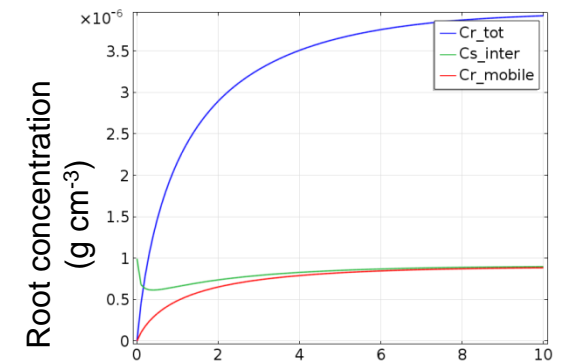
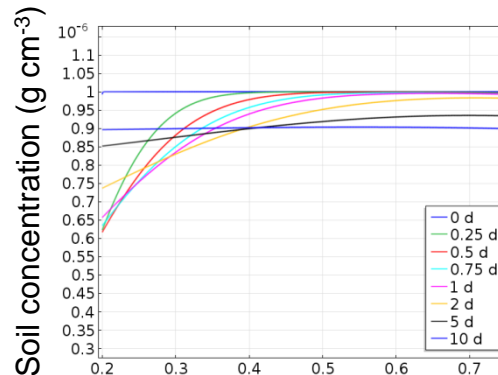
Case 1: No gradient



Case 2: Accumulation



Case 3: Depletion



r-coordinate (cm)

Time (d)

Conclusion

- Gradients develop within the first 0.5 cm
- This study can be used to estimate voxel discretization for numerical models
- Root-soil interface gradients cannot be neglected for all model parameterizations
- Different general types of gradients at the root-soil interface can be distinguished already by comparing the relevant model parameters.



Thank you!