# Inorganic Materials Chemistry and Nanomaterials Core Module 9









### **Inorganic Materials Chemistry and Nanomaterials**

### 8 lectures Module 9

### **Synopsis**

- 1. Structural concepts: Dimensionality, defects and non-stoichiometry
- 2. Dynamics in solids: Batteries and dielectric materials
- 3. Magnetic Materials: Paramagnetism and Cooperative magnetism
- 4. Metals and Superconductivity: Electronic conduction.
- 5. Nanomaterials: Synthesis, characterisation and structure
- 6. Nanomaterials: Properties and applications

### **Bibliography:**

M. T. Weller

Н	М	Rosenberg	'The	hiloe	state'
11.	IVI.	17095110514	1110	SUIIU	State

'Solid state chemistry and its applications' A. R. West

'Solid state chemistry. An introduction' L. Smart and E. Moore A. K. Cheetham and P. Day

'Solid state chemistry. Techniques'

'Inorganic materials chemistry'

'Inorganic Chemistry'

### **Associated Courses**

Shriver and Atkins

AKD	Transition metals	1 <sup>st</sup> year
MAB	Solid state structure	1 <sup>st</sup> year
JML	Structure and bonding	1 <sup>st</sup> year
RED	Metal-ligand bonding	2 <sup>nd</sup> year
TD	Processes at solid surfaces	3 <sup>rd</sup> year
NTH	Photochemistry	3 <sup>rd</sup> year
KDC	Diffraction	3 <sup>rd</sup> year

### Learning Objectives: by the end of the course you should be able to

- i) explain structure types and polymorphism.
- ii) explain the main reasons for and types of defects in ionic solids.
- iii) calculate the proportion of defects in a solid.
- iv) explain what is meant by a non-stoichiometric solid and a solid solution.
- v) understand the principles of a battery and calculate energetics
- vi) describe the perovskite structure and its relation to ferroelectricity using the tolerance factor.
- vii) describe the phenomenon of piezoelectricity and pyroelectricity.
- viii) understand and explain the behaviour of a paramagnet, antiferromagnet, ferromagnet and ferrimagnet as a function of temperature.
- ix) explain the effect of domain structure of ferro- and ferrimagnets.
- x) explain the superexchange mechanism for rock salt metal oxides.
- xi) describe the spinel structure and estimate the net magnetic moment of ferrimagnets.
- xii) Understand basic models of electrical conductivity in metals and semiconductors, Fermi energy/level, density of states, and semiconductor doping.
- xiii) describe the electric and magnetic properties of superconductors.
- xiv) explain the structural characteristics of cuprates, fullerides and borides.
- xv) qualitatively describe BCS theory of superconductivity and the relationship between  $T_c$  and atomic mass.
- xvi) understand the structural differences between bulk materials and nanomaterials.
- xvii) describe methods of synthesis of solid state compounds using examples.
- xviii) understand the difference between synthesis and modification of materials.
- xix) describe the use of diffraction, microscopy and spectroscopic methods used to characterise (nano)materials.
- xx) understand the limitations of techniques for the analysis of (nano)materials.
- understand the relationship between the size of nanoparticles and their physical properties.

#### Introduction

### What is materials (solid state) chemistry?

Solid state chemistry is concerned with the synthesis, structure, properties and application of solids including inorganic and organic materials and their composites.

At the interface of chemistry, solid state physics, materials science, ceramics, mineralogy and metallurgy.

### Why is materials (solid state) chemistry important?

Society and technology are underpinned by the solid state sciences. For example

Computing (data storage, CD lasers, batteries, metals, semiconductors)

Construction (concrete, steels)

Transport (catalytic converters, fuel cells, strong lightweight materials)
Chemicals (catalysts, sensors, coatings, additives)
Medicine (artificial joints, bones, and muscle)
Gems (jewellery, cutting tools, lasers)

Energy (Solar panels (metals and semiconductors), wind turbines, batteries, nuclear fission, and fusion containment)









The function of a material is dependent on the structure and composition

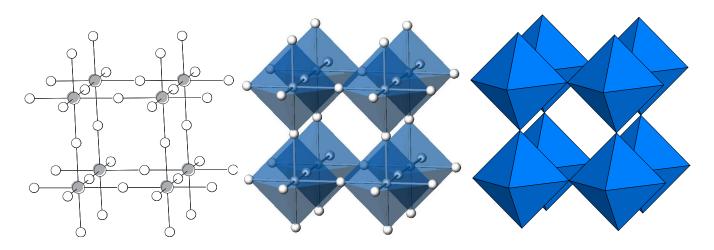
### **Structural Concepts**

### 1. Crystallinity

Solids exhibit a continuum of order from perfect crystals to totally amorphous. long range order = crystalline (e.g.  $SiO_2$  as quartz) short range order = amorphous (e.g.  $SiO_2$  as glass).

### Structure types

Structures of compounds can be divided into classes. Traditionally each class is named after an archetypal compound or mineral.

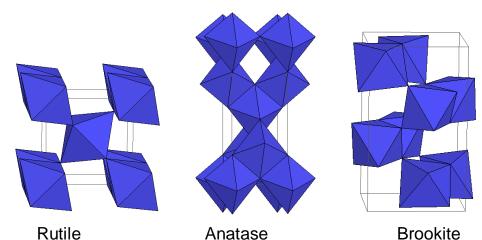


'ball and stick' and polyhedral representations of ReO3 structure type

e.g.1 ReO $_3$  is built from vertex sharing ReO $_6$  octahedra. Any other compound that exhibits this type of structure (e.g. NbF $_3$ ) is called a *structure type*. NbF $_3$  has the ReO $_3$  structure type.

e.g.2 The rock salts. These are simple cubic structures that many alkali metal halides adopt e.g. NaCl. NaCl has the rock salt structure type.

# 2. Polymorphism



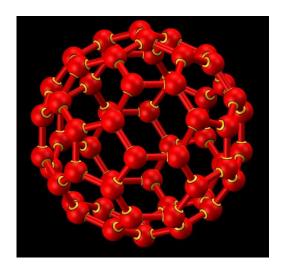
Some elements have allotropes e.g. C (graphite, diamond, fullerenes) and some molecular compounds have isomers e.g. (alkanes).

Some solid compounds can also have more than one crystalline structure for a single stoichiometry. This is called *polymorphism* and individual structures are called *polymorphs*. Rutile, anatase and brookite are all polymorphs of TiO<sub>2</sub>. Individual polymorphs will be thermodynamic stability at a particular pressure and temperature, but other polymoprhs can have kinetic stability at the same pressure and temperatures

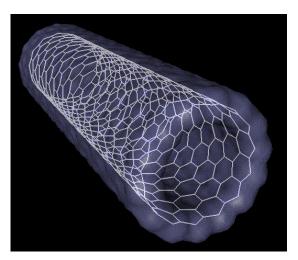
Often a solid having a particular crystalline structure and stoichiometry is referred to as a *phase*.

### 3. Dimensionality and porosity

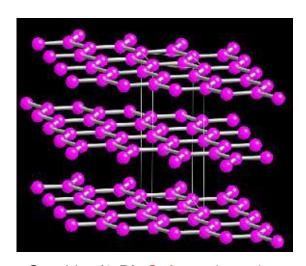
**Dimensionality** is important in understanding the properties of solids. e.g.  $C_{60}$ , nanotubes, graphite and diamond.



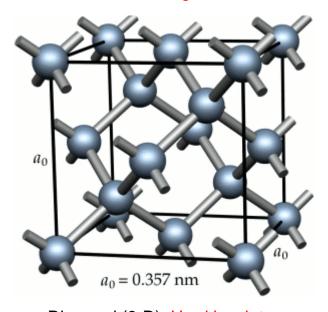
C<sub>60</sub> (0-D). Soluble molecule.



Carbon nanotube (1-D). Semiconductors. Immense tensile strength.

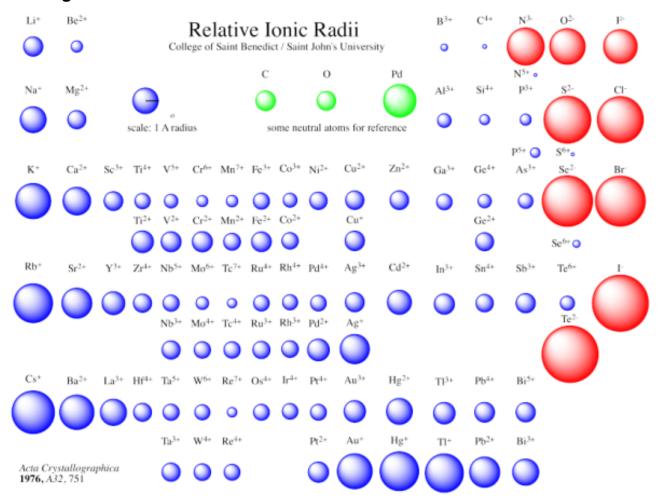


Graphite (2-D). Soft semimetal.



Diamond (3-D). Hard insulator.

### Some general notes on structure



1. For ionic structures (e.g. oxides, halides, silicates) the anions are much bigger than the cations. Therefore,

the anions are close packed and the cations fit into the interstitial sites. the cations will be more mobile.

- In drawings for solid structures lines between atoms do not always mean there is a localised bond. Particularly in ionic compounds the lines describe coordination (nearest neighbours).
   However, many ionic compounds do have some covalent character which can be used to understand properties.
- 3. The overall charge of a bulk solid will be zero. However, charge can be distributed heterogeneously (e.g. in a dielectric (see later))

## 4. Defects and non-stoichiometry

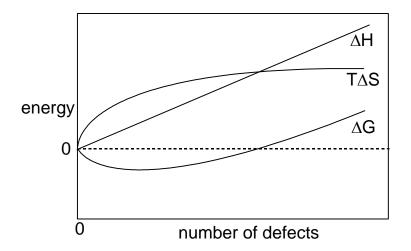
Note: overall charge balance must be maintained.

Only at 0 K will an ionic crystal have a perfectly ordered array of atoms where every atomic lattice point contains an atom.

At > 0 K crystals contain defects. Defect formation requires energy and is always endothermic. However a structure with defects has higher entropy.

Increased entropy drives defect formation to  $\Delta G = 0$  (equilibrium).

Remember  $\Delta G = \Delta H - T\Delta S$ . Strong temperature dependence on the number of defects.



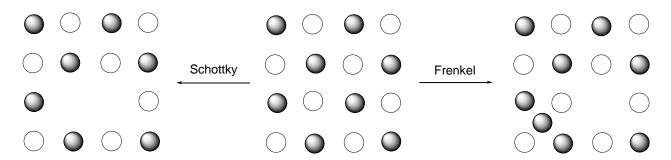
### Point defects (intrinsic)

Vacancy: An ion is missing

Interstitial: an extra ion is present in an interstitial site Schottky: a pair of vacancies are present in the lattice.

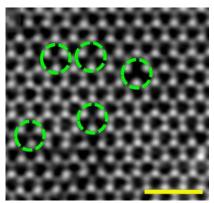
Frenkel: a defect pair is created by an ion (usually cation) moving into an interstitial site.

The lattice will distort at the vacancy site to minimise the loss in lattice energy. Vacancies or interstitial atoms do not have to be adjacent and can be mobile.



Proportion of defects 
$$\underline{n_{S(F)}} = \exp(-\Delta H_{S(F)}/2kT)$$

Where  $n_S$  ( $n_F$ ) = Shottky (Frenkel) defects per unit volume,  $\Delta H_S$  (( $\Delta H_F$ ) = Shottky (Frenkel) enthalpy of formation, N = number of cation and anion sites per unit volume.



TEM of S vacancies in  $MoS_2$  (scale bar 1 nm) (J. Hong et al, Nature Commun. **2015**, <u>6</u>, 6293)

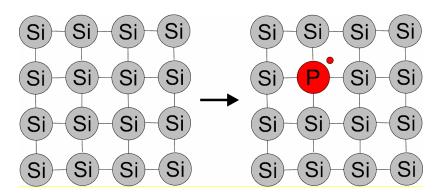
Temperature (K)	Compound (defect)	ΔH (10 <sup>-19</sup> J)	n/N
300	MgO (S)	10.57	3.62 x 10 <sup>-56</sup>
300	CaO (S)	9.77	5.69 x 10 <sup>-52</sup>
300	LiF (S)	3.75	2.14 x 10 <sup>-20</sup>
300	LiCl (S)	3.40	1.46 x 10 <sup>-18</sup>
300	LiBr (S)	2.88	7.83 x 10 <sup>-16</sup>
300	Lil (S)	2.08	1.23 x 10 <sup>-11</sup>
300	β-AgI (cation F)	1.12	1.33 x 10 <sup>-6</sup>
500	LiCl	3.40	1.99 x 10 <sup>-11</sup>
750 LiCl		3.40	7.35 x 10 <sup>-8</sup>
1000 LiCl		3.40	4.46 x 10 <sup>-6</sup>

The percentage of intrinsic point defects in most ionic compounds is small but they can have a significant effect on electrical, magnetic and optical properties. The smallest  $\Delta H$  ( $\Delta H_S$  or  $\Delta H_F$ ) will determine if Schottky or Frenkel defects dominate.

### Point defects (extrinsic)

Introducing different ions into the structure. This is known as *doping*.

Silicon (group 14) is not a good conductor of electricity. If Si is doped with small amounts (1%) of P (group15) the conductivity increases significantly as an occupied state is introduced just below the Si conduction band. In effect after forming bonds to silicon the remaining electron from P acts as a conduction electron.



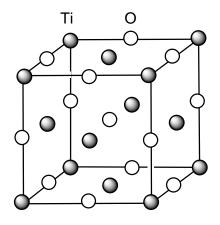
### Non-stoichiometry and solid solutions

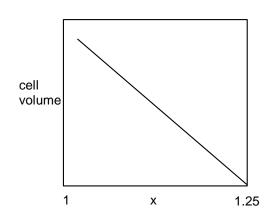
Defects and doping result in non-stoichiometric solids. e.g.  $YBa_2Cu_3O_{7-x}$  (0<x<1). Non-stoichiometry is common for compounds of transition metals that can have variable oxidation state.

e.g. TiO is non-stoichiometric. It has the rock salt structure over the range  $TiO_x$  (where 0.7 < x < 1.25).

Non-stoichiometric compounds are distinct from other compositions e.g. TiO<sub>2</sub> because they have a common structure.

However the lattice parameters (size of the unit cell) of the structure will change gradually as the ratio of elements changes.





Consider that TiO<sub>1.25</sub> can be rewritten as Ti<sub>0.8</sub>O. Is the non-stoichiometry due to extra oxygen present in interstitial sites or vacancies on the titanium site?

### From experimental evidence

At x < 1 oxygen vacancies are present in the structure

At x > 1 titanium vacancies are present in the structure

TiO has both Ti and O vacancies!

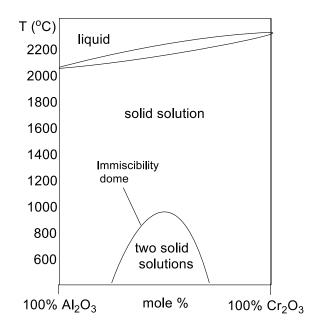
What is the average oxidation state of Ti in  $TiO_{1.25}$ ?

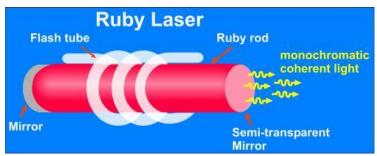
 $Ti^{2.5+} = 50:50$  mixture of  $Ti^{2+}$  and  $Ti^{3+}$ 

**Solid solutions** are commonly observed in non-stoichiometric solids. A solid solution is a crystalline solid that can have continual variable composition for a given structure type. They are a useful method of discovering and fine-tuning properties. e.g. lasers and steel.

There are two types: <u>substitutional</u> where a new atom replaces an existing atom. e.g. by doping, and *interstitial* where an atom is added to an interstitial site.

Substitutional  $Al_2O_3$  and  $Cr_2O_3$  can form a solid solution over the compositional range  $(Al_{2-x}Cr_x)O_3$  0 < x < 2. x < 0.05 (ruby)





Interstitial. e.g. C in Fe giving  $FeC_x$  0 < x < 0.09 (C atoms occupy the interstitial sites of Fe). (steel).



The Forth Bridge

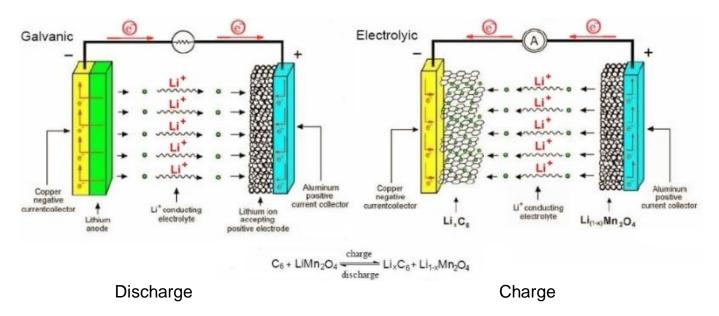
### **Dynamics in solids**

Above 0 K, atoms and ions in compounds move and respond to external stimuli (e.g. magnetic and electric fields, pressure and temperature).

### Long range movement of ions (μm-mm)

batteries and fuel cells

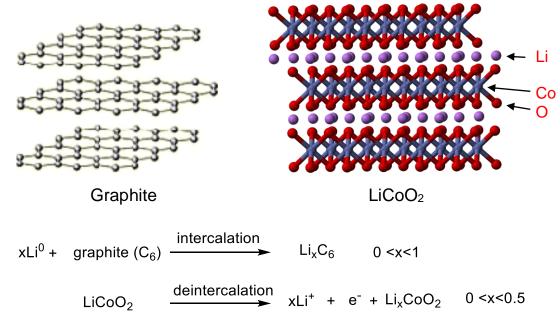
### Lithium ion batteries (rechargeable) (Nobel Prize 2019)



Batteries comprise two electrodes and an electrolyte (+membrane and connector-contacts). The Li<sup>+</sup> must be mobile in all the electrodes and electrolyte materials.

### Intercalation/deintercalation

Species can be added/removed from a host structure. Needed for charge/discharge cycles. Important structural features: layers, channels or porosity provide space for Li<sup>+</sup> to move.



### **Energetics**

 $E_{cell}(V) = E_{cathode} - E_{anode}$ Power (W) = voltage (V) x current (A) Charge (Ah) = current (A) x time (h) 1 Ah = 3600 C

Energy (Wh) = Power (W) x time (h) 1 Wh = 3600 J Energy density = Energy stored per unit battery volume (Wh L<sup>-1</sup>) Specific energy = Energy stored per unit battery weight (Wh kg<sup>-1</sup>)

### **Examples**

AA battery (1.5V, 3 Ah) = 4.5 Wh Lead Acid (12 V, 50 Ah) = 600 Wh Lithium Ion battery laptop (10 V, 5 Ah) = 50 Wh Toyota Prius battery (202 V, 6.5 Ah) = 1300 Wh c.f. Tank of petrol = 600,000 Wh

e.g. For a lithium battery during discharge

$$E_{cell} = 1 - (-3) = 4V$$
 
$$\Delta G = -nFE \ (F = 96500 \ C \ mol^{-1}) = -386000 \ J \ mol^{-1} = -107.2 \ Wh \ mol^{-1}$$
 
$$LiC_6 = 79 \ g \ mol^{-1}, \ CoO_2 = 91 \ g \ mol^{-1}$$
 Theoretical specific Energy = -107.2/0.170 = 630.6 Wh kg<sup>-1</sup>

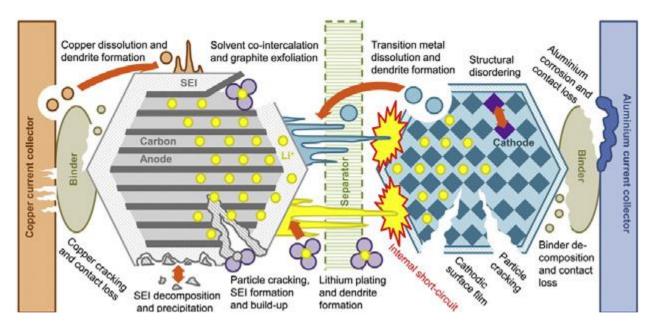
In reality about 30% is achieved ~ 190 Wh kg<sup>-1</sup> because of resistivity losses and the extra weight of terminals, case, separators etc.

### **Challenges**

Battery science is a complicated chemical and engineering problem

### Goals

Maximise energy density and/or specific energy with long life Cheap manufacturing/recycling using sustainable elements



Potential Problems (Journal of Power Sources 2017, 341, 373 – 386)

Intercalation/deintercalation should not result in big structural changes leads to mechanical stress, fracture and performance loss

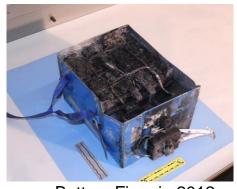
Avoid uncontrolled Li metal growth (dendrites) leads to shorting and probable ignition of the flammable electrolyte.

Interfaces between electrodes and electrolyte are critical. (solid electrolyte interface (SEI)) growth of secondary layer on electrodes usually helps to prevent degradation of electrolyte on contact with strongly reducing and oxidizing electrodes and growth of Li dendrites.

# Kinetics of charge and discharge are also critical (fast charge/discharge) But not too fast!



**Boeing Dreamliner 787** 



Battery Fires in 2012

# Localised movement of ions (pm)

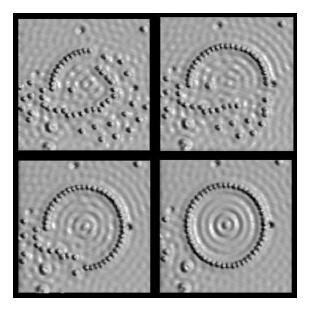
electronics

(capacitors (in all electronic devices), switching, radio, radar) transducers

(sound generation (sonar and ultrasound), measurement (e.g. light and pressure sensors), time keeping)

Many scientific instruments

(spectrometers, microbalances, electron microscopy and atom manipulation)



'Quantum coral' 48 Fe atoms positioned on a Cu(111) surface.

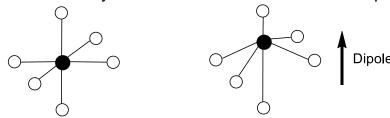
Crommie et al, *Science*, 1993, 262, 218

How is it possible to manipulate individual atoms with pm precision? Piezolelectric materials (also used to generate ultra sound)



Ultrasound Scan (Douthwaite et al, 2014)

When an ion is in an asymmetric site there will be a local dipole moment.



To obtain a bulk polarisation (P) the material must have a non-centrosymmetric crystal structure otherwise the local dipoles cancel out.

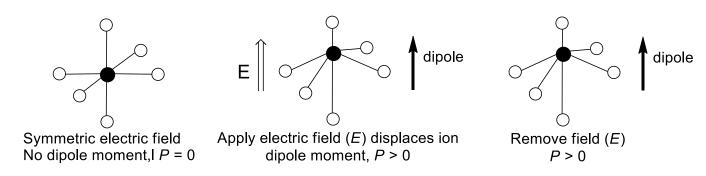
Any process that changes the relative position of ions will change the polarisation.

**Ferroelectrics**-dipoles respond to an electric field (energy storage (electrical potential))

**Piezoelectrics**-dipoles respond to pressure (convert kinetic to electrical potential and vice versa)

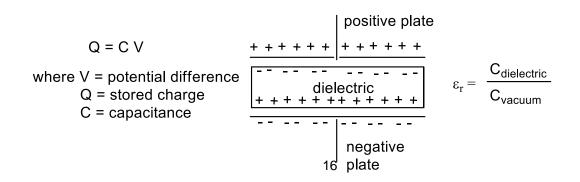
**Pyroelectrics**-the dipoles respond to heat (photons) (convert heat to electrical potential)

**Ferroelectrics** can retain polarisation (P) after the electric field has been removed and have a very high dielectric *permittivity*,  $\varepsilon_r$ .



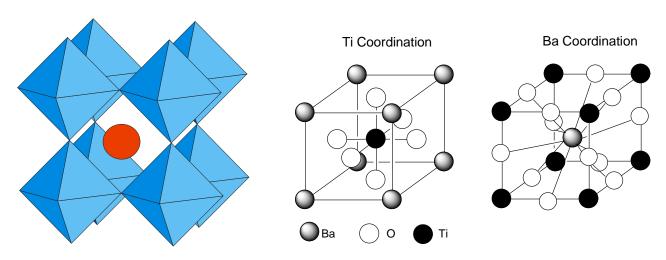
A good dielectric material should have high *dielectric strength* (not breakdown at high voltages and become electron or ion conducting) and have low dielectric loss (not lose electrical energy as heat in an alternating electric field).

The stored charge can be measured in a parallel plate capacitor and the dielectric permittivity ( $\epsilon_r$ ) determined.



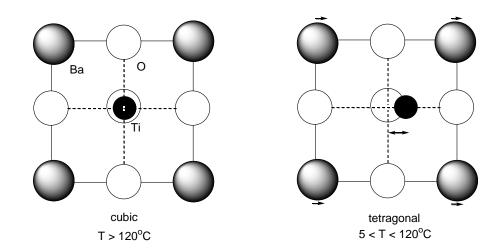
An example of a ferroelectric is BaTiO<sub>3</sub> that has the perovskite ABO<sub>3</sub> structure (related to ReO<sub>3</sub>).

$$\varepsilon_{\rm r} \, {\rm BaTiO_3} = 10^2 - 10^4$$



At temperatures above 120°C the Ti atoms are in a symmetric octahedral TiO<sub>6</sub> site (cubic BaTiO<sub>3</sub> (centrosymmetric)).

Between 5 - 120°C the Ti atoms are displaced along one of the axis of the octahedron (by 0.1 Å) and polarisation results (tetragonal BaTiO<sub>3</sub> (non-centrosymmetric)).



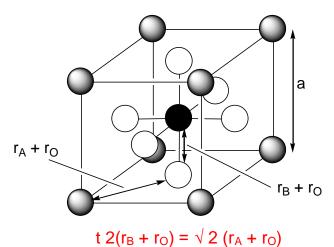
# Why does the structure distort?

The structure of a compound is dependent on the size, charge and preferred coordination number/geometry of the constituent ions.

For compounds that contain several elements the ideal preferences for each ion may not be accommodated and strain may be present. Significant strain will result in a structural distortion.

For transition metal oxides distortions can be estimated using a tolerance factor.

Consider the perovskite ABO<sub>3</sub> structure.



From the diagram it can be seen that 
$$a = 2 (r_B + r_O)$$
 and  $a = \sqrt{2} (r_A + r_O)$ 

Therefore to obtain ideal contact between A. B and O

$$2 (r_B + r_O) = \sqrt{2 (r_A + r_O)}$$

Some deviation from this ideal can be included by introduction of a *tolerance factor* t.

For the ideal structure t = 1. As t deviates from 1 strain is introduced due to one or both of the cations not fitting properly. 0.85 < t < 1.06 gives a distorted perovskite. Outside this range a non-perovskite structure is usually adopted.

e.g.  $SrTiO_3 Sr^{2+}$  (r = 158 pm),  $Ti^{4+}$ (r = 74.5 pm),  $O^{2-}$  (r = 126pm) t = 1.002 (good fit, almost ideal)

BaTiO<sub>3</sub> Ba<sup>2+</sup> (r = 175 pm), t = 1.06 (Ti ion is occupying a site larger than it would prefer, strain)

At  $T > 120^{\circ}C$  the thermal motion of the Ti atom creates enough chemical pressure to retain the ideal cubic perovskite structure.

At 5 < T < 120°C the thermal motion no longer compensates for the strain and the structure distorts.

The polarisation can be removed and reversed by application of an opposing electric field. Ferroelectrics exhibit hysteresis which allows charge to be stored and their use in capacitors.



D b b E(V)

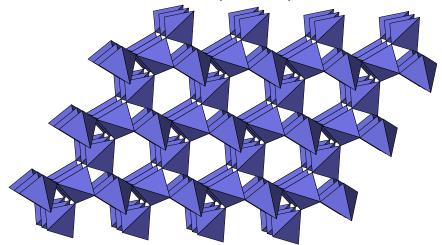
a to b. Apply electric field and individual dipoles are aligned. At b the sample has reached *saturation polarisation*.

b to c. Electric field is returned to 0 but the sample remains polarised this is known as the *remanent polarisation*.

c to d In order to depolarise the sample a field in the opposite direction is required. This is the *coercive field*.

**Piezoelectrics** polarise under the action of mechanical stress and develop electrical charges on opposite crystal faces (i.e. a voltage difference). Conversely when an electric field is placed across a piezoelectric crystal it develops strain.

Many compounds composed of tetrahedral groups distort under stress and are peizoelectric. Also tetrahedra do not have a centre of symmetry and often lead to non-centrosymmetric structures. An example is  $\alpha$ -quartz.



Piezoelectrics are used extensively as transducers for loudspeakers, earphones, inkjet printers, STM (see later), cigarette lighters etc

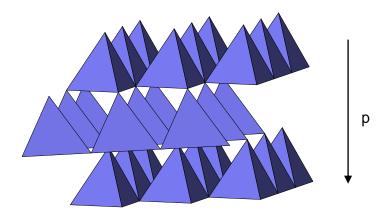
If an alternating electric field is applied to a piezoelectric the crystal will vibrate. Resonance occurs if the vibration corresponds to a fundamental mode of the crystal. This oscillation is the basis of using quartz for timekeeping.



Lighter watch (two piezoelecrics in action!)

**Pyroelectrics** exhibit a net bulk spontaneous polarisation that is temperature dependent. Thermal expansion or contraction of the lattice changes the size of the dipoles.

An example of a pyroelectric material is ZnO that has the wurtzite structure.



The ZnO<sub>4</sub> tetrahedra (dipoles) point in the same direction, giving rise to a net bulk polarisation. In contrast to ferroelectrics the polarisation of pyroelectrics cannot usually be reversed by the action of an electric (coercive) field.

Pyroelectrics are used in systems where an electrical response to temperature is useful. e.g. infrared radiation detectors (night vision and PIR (passive infra-red) motion sensors), spectrometers and temperature sensors.



Security PIR sensor

### **Magnetic Materials**

Transition metals and lanthanides can have partially filled valence orbitals that result in unpaired electrons and magnetism. For materials, the collective interaction of the ions is key. The strength and direction of the interaction will depend on the spatial relationship (crystal structure) between the ions and the mechanism for magnetic exchange (exchange interaction). The angular momentum (J) of unpaired electrons gives rise to magnetic behaviour. Magnetic behaviour is a quantum mechanical phenomenon.

Nobel Prize (1970, 1977, 1982, 2007)

Magnetic memory
(security strips, hard drives)
Power generation
(transformer cores, motors)
Sound generation
(loudspeakers, microphones)

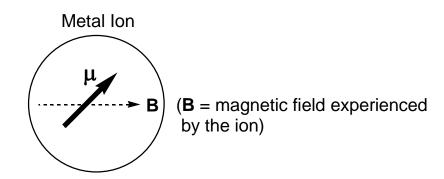








### Magnetism of individual ions



On the microscopic level individual ions with unpaired electrons have a magnetic dipole moment  $\mu$  (sometimes called spin). The size of  $\mu$  depends on the spin and orbital angular moments. (see *f*-elements course)

$$\mu_{S} = g \sqrt{(S(S+1))}$$

$$\mu_{S+L} = \sqrt{(4S(S+1) + L(L+1))}$$

Spin only formula

Includes spin orbit coupling (Russell-Sanders coupling)

S = total spin angular momentum (No. electrons/2), L = total orbital angular momentum, g = g-factor (free electron value ~2 can be used when L = 0)

ion	Unpaired electrons	μ <sub>S</sub> (calc)	μs+L (calc)	μ <sub>eff</sub> (observed)
V <sup>4+</sup>	1	1.73	3.00	~ 1.8
V <sup>3+</sup>	2	2.83	4.47	~ 2.8
Cr <sup>3+</sup>	3	3.87	5.20	~ 3.8
Mn <sup>2+</sup>	5 (high spin)	5.92	5.92	~5.9
Fe <sup>2+</sup>	4 (high spin)	4.90	5.48	5.1 – 5.5
Co <sup>2+</sup>	3 (high spin)	3.87	5.20	4.1 – 5.2
Ni <sup>2+</sup>	2	2.83	4.47	2.8 - 4.0
Cu <sup>2+</sup>	1	1.73	3.00	1.7 – 2.2

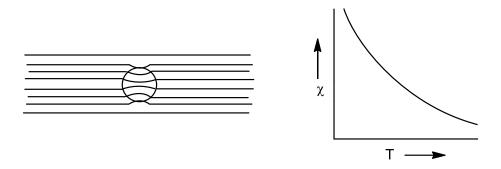
The orbital angular momentum is due to the motion of the electron about the nucleus. In many compounds (particularly the first row) the orbital angular momentum is almost entirely quenched because the *d*-orbitals are no longer degenerate.

For heavier transition metals and the actinides the spin-orbit coupling is large and Russell-Sanders coupling inappropriate. Use j-j coupling scheme instead. Large spin-orbit coupling can give rise to very large moments. We shall not consider j-j coupling any further.

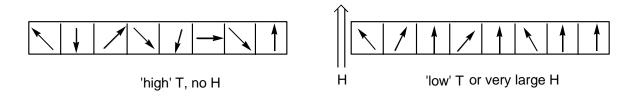
# Collective (bulk) magnetism

The magnetic susceptibility  $\chi$  is a measure of how magnetic a material is.  $\chi$  varies with temperature (and applied external magnetic field) for different types of magnetism. (basis of technological applications of magnets)

**Paramagnetism** is observed for compounds that contain unpaired electrons and where the magnetic dipoles do not interact with each other. A paramagnet is attracted to an external magnetic field.

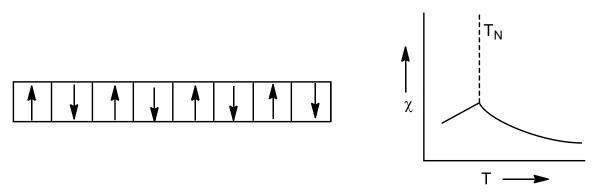


As the temperature decreases the dipoles can begin to align (order) parallel (lowest energy configuration) to an external field.



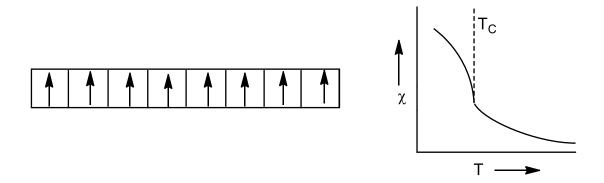
Paramagnetism is temperature dependent.

**Antiferromagnetism** is an example of cooperative magnetism where no applied field is necessary to align dipoles (spins) anti-parallel.



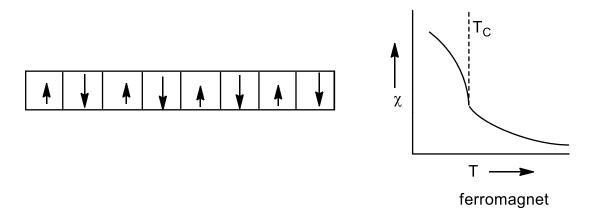
T<sub>N</sub> is the Néel temperature (antiferromagnetic-paramagnetic transition temperature)

**Ferromagnetism** is an example of cooperative magnetism where no applied field is necessary to align spins parallel.



T<sub>C</sub> is the Curie temperature (ferromagnetic-paramagnetic transition temperature).

**Ferrimagnetism** is an example of cooperative magnetism where no applied field is necessary to align spins. The alignment is essentially non-parallel giving partial cancellation of 'up' and 'down' spins.



# The Exchange Interaction

### **Ferromagnetism**

Is usually associated with metals that have an electronic band structure.

There are only a few elements that are ferromagnetic Fe, Co, Ni, Gd and Tb.

We will not consider the magnetism of metals

### **Antiferromagnetism and Ferrimagnetism**

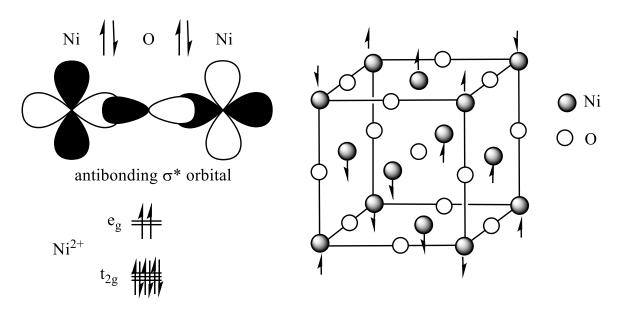
### Superexchange

Superexchange is where anions mediate magnetic exchange between metal cations. Anions can be sulfur and fluorine but more commonly oxygen.

Superexchange occurs via overlap of atomic orbitals of the oxygen (p) and metal (d) atoms.

### Superexchange leading to Antiferromagentism

e.g. First row transition metal monoxides such as NiO and MnO adopt the rock salt structure where the metal and oxygen are in octahedral sites.



Two  $e_g$  ( $d_{x2-y2}$  or  $d_z^2$ ) orbitals containing an unpaired electron overlap with an  $O^{2-}p$  orbital that contains two oppositely aligned electrons. The spins align themselves to be antiparallel giving an overall antiferromagnetic exchange coupling.

Effectively there are two Ni lattices that contain Ni spins 'up' and one 'down'. Each of these is know as a sublattice. Below  $T_N$  the sublattice structure of NiO can be determined experimentally using neutron diffraction (see later).

Above  $T_N$  thermal energy is greater than the superexchange interaction and the spins no longer align giving paramagnetic behaviour.

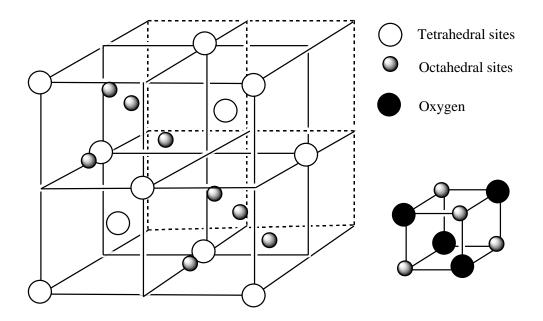
### Superexchange leading to Ferrimagnetism

We need a structure that can have at least two types of ions, either different elements or oxidation states that that have different magnetic moments and can occupy unique crystallographic sites. Consider an antiferromagnet that has two unique sublattices but where the magnetic moment of one sublattice is greater than the other.

Ferrimagnets are very important industrial materials because they have similar properties to ferromagnets, but are electrically insulating.

A crystal structure is required that has two different metal sites. This is found in the spinel and inverse spinel structure type.

Spinel is the name given to a structure type of the formula AB<sub>2</sub>X<sub>4</sub> e.g. MgAl<sub>2</sub>O<sub>4</sub>.



The structure is based on a cubic close packed array of anion atoms.

The spinels and inverse spinels are then constructed by filling 1/8 of the tetrahedral and  $\frac{1}{2}$  of the octahedral sites in an ordered manner.

 $[A^{2+}]^{tet} [B^{3+}]^{oct} \qquad [B^{3+}]^{tet} [A^{2+}, B^{3+}]^{oct} \\ MgAl_2O_4 \qquad CoFe_2O_4 \\ BaFe_2O_4 \text{ (credit card strips, speakers} \qquad NiFe_2O_4 \\ Mn_3O_4 \qquad Fe_3O_4 \text{ (magnetite) (loadstone)}$ 

Not all spinels have clear preference of metal ions for particular coordination sites. Many examples contain mixed metal sites. e.g. MnFe<sub>2</sub>O<sub>4</sub> contains 80% normal and 20% inverse.

The preference for normal or inverse spinel is due to several factors.

- 1. From electrostatics M<sup>3+</sup> should prefer the octahedral site and M<sup>2+</sup> the tetrahedral site.
- 2. The smaller cation would generally go in the smaller tetrahedral site
- 3. Crystal field stabilisation energies (CFSE). Which ion prefers the Oh site?

# e.g. NiFe<sub>2</sub>O<sub>4</sub>

Oxide lattice provides a weak field for the metal atoms.

Must be 1 x Ni(II) and 2 x Fe(III). Fe(III) d<sup>5</sup> are high spin. No preference for Oh or Td based on CFSE. CFSE for Ni in octahedral > tetrahedral. Therefore Ni goes in octahedral site to give the inverse spinel structure.

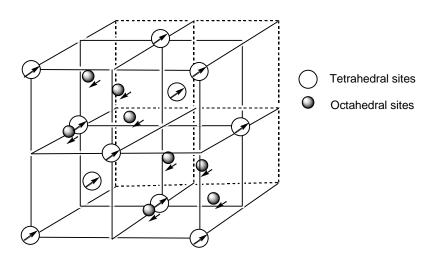
### Estimation of the magnetic moment of ferrimagnets

Using  $\mu = gS$  as a rough estimate (instead of  $\mu_S = g \sqrt{(S(S+1))}$ ) we can calculate the magnetic moment  $\mu$  for each ion. The saturation (maximum) magnetic moment ( $\mu_{Sat}$ ) for a ferrimagnet is then a vector sum of the individual ion moments.

We need to know how the spins couple with respect to each other.

- 1) The coupling between octahedral site ions is weak. Between tetrahedral sites also weak.
- 2) Superexchange between the octahedral and tetrahedral ions is strong giving antiferromagnetic alignment.

Therefore all A moments in same direction and all B moment in same direction (but opposite to A)



# e.g. NiFe<sub>2</sub>O<sub>4</sub> (inverse spinel)

ion	[Ni <sup>2+</sup> ] <sup>oct</sup> , d <sup>8</sup>	[Fe <sup>3+</sup> ] <sup>oct</sup> , d <sup>5</sup>	[Fe <sup>3+</sup> ] <sup>tet</sup> , d <sup>5</sup>	μtot
No. unpaired	2	5	5	
electrons				
μion	2	5	5	2 + 5 - 5 = 2

Comparison of estimation and experimental data for M <sup>II</sup> Fe <sup>III</sup> <sub>2</sub> O <sub>4</sub>					
M(II)	S	μsat calc	μsat expt	T <sub>N</sub>	Discrepancy
Mn	5/2	5	4.55	573	90% normal
Fe	2	4	4.1	858	s.o. coupling
Co	3/2	3	3.94	793	s.o. coupling
Ni	1	2	2.3	858	s.o. coupling
Cu	1/2	1	1.3	726	s.o. coupling
Mg	0	0	1.1	713	90% inverse

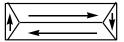
### **Domains**

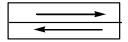
Fe has a  $T_C$  of 1043K. Why are not all Fe objects magnetic at room temperature? Why does placing a magnet next to Fe magnetise it? How can BaFe<sub>2</sub>O<sub>4</sub> be used to store magnetic data?

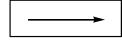
Below T<sub>C</sub> magnet materials are divided into *domains*.

Each domain has ions aligned in parallel, but in the absence of an external magnetic field the domains are not parallel to each other. Entropy drives the formation of domains.

On the application of an external magnetic field (H) the domains align in the same direction as the field.

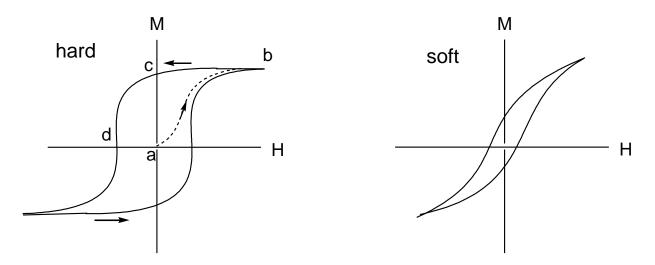






When all the domains are parallel the magnetisation M is at a maximum (*saturation magnetisation*). M is the magnetic dipole moment per unit volume.

These M vs H diagrams are known as hysterisis curves



The domains can be aligned in any direction by changing the direction of the external field. Aligning and changing the direction of domains requires energy.

a to b. The domains of a sample are aligned in a magnetic field. At b the sample has reached *saturation magnetisation*.

b to c. The field is returned to 0 but the sample remains magnetised this is known as the *remanent magnetisation*.

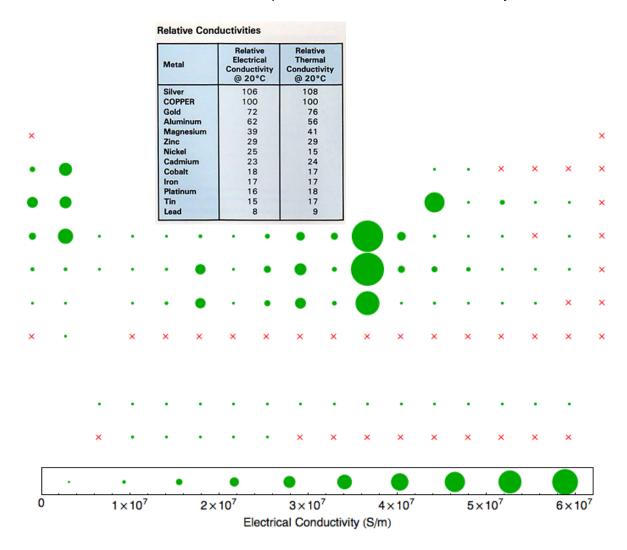
c to d In order to demagnetise the sample a field in the opposite direction is required. This is called the *coercive field*.

A hard magnet has a large remanent magnetisation and large coercive field: used as permanent magnets and magnetic memory (BaFe<sub>2</sub>O<sub>4</sub>).

A soft magnet has a small remanent magentisation and a small coercive field: used as transformer cores (Si doped Fe).

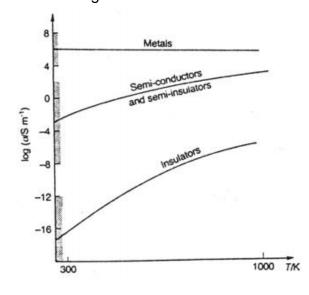
# **Electrical Conductivity**

All materials can be classified with respect to their electrical conductivity.



# Conductivity ( $\sigma$ ) as a function of temperature

Note the log scale



Insulator:  $\sigma < 10^{-9} \text{ Sm}^{-1}$ . Conductivity increases with Temp.

Semiconductor:  $\sigma = 10^{-3} - 10^{3}$  Sm<sup>-1</sup> Conductivity increases with Temp.

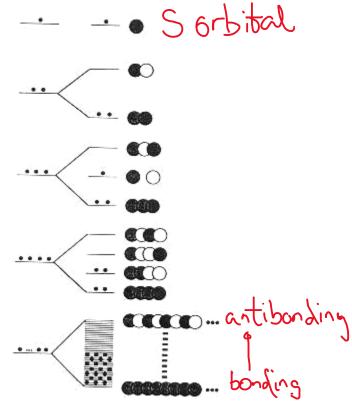
Metal:  $\sigma > 10^7 \, \text{Sm}^{-1}$ 

Conductivity decreases with Temp.

Can we explain the trends in conductivity?

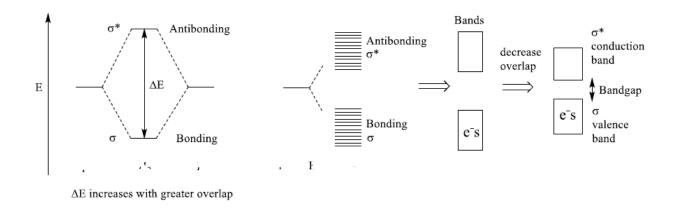
### **Band Theory**

(Overlap of large numbers of atomic orbitals. Extension of LCAO-MO theory)



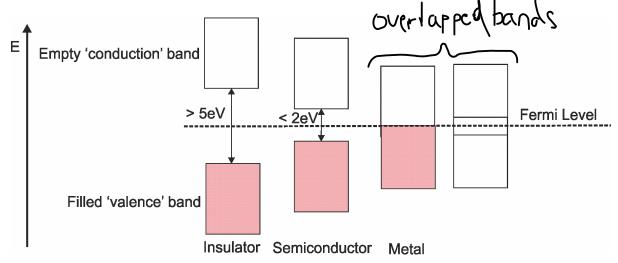
Band orbitals are not distributed evenly in a band. There are fewer at the band edges. The number of orbitals (states) per unit energy is called the density of states N(E). The density of states is lower at the band edges.

For some materials the bonding and antibonding bands split (like in a molecule) giving an energy gap (band gap)



The band width (energy range), band structure (distribution of orbitals), and band gap will depend on the orbitals, structure and bonding (e.g. metallic, ionic, or covalent). A key parameter is orbital overlap, which can be interpreted very similarly to metal-ligand bonding in metal complex coordination chemistry (see yr 2 course M-L bonding).

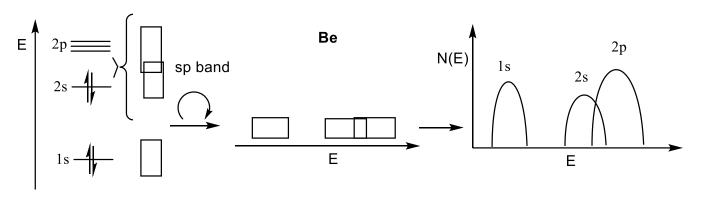
**General description of Insulators, Semiconductors and Metals** 



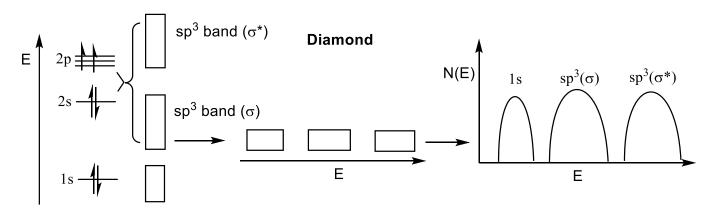
Fermi level is the energy with a 50% probability of electron occupation under any conditions. Very important concept (see below).

### Bands from s, p and d-orbitals

e.g. Be (hcp structure) vs C (diamond structure)



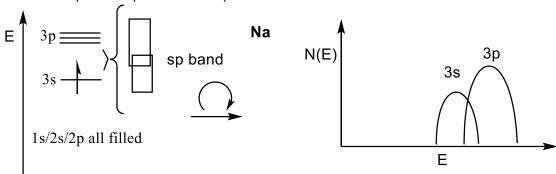
Overlap of 2s and 2p valence orbitals gives a single band. The band is partially filled with electrons. Be is a metal.



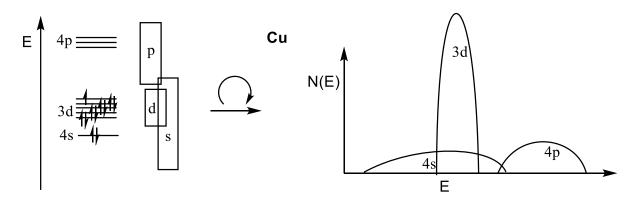
Overlap of 2s and 2p valance orbitals gives two bands (sp<sup>3</sup> bonding and antibonding bands).

The lower band is completely filled with electrons. Diamond is an insulator

Na (bcc structure) vs Cu (fcc structure)



Essentially a half filled 3s band Na is a metal.



d-band is very narrow and has a high density of states (lots of orbitals and electrons).

For Cu electron filling at 3d/4s boundary. Other transition metals will be filled within the d-band (< group 11) or sp band (> group 11). Cu is a better conductor than Na.

### Orbital dependence on conductivity

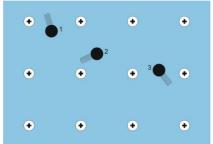
Electron delocalisation increases conductivity

Orbital overlap, energy and shape are key (cf molecular bonding)

s-orbitals are isotropic = good delocalisation.

Heating a metal reduces orbital overlap and the ions vibrate more (decrease conductivity)

Simple free electron model for a metal



Similar to ideal gas. Electrons are able to move without interacting with the positive lattice or each other (Fermi gas).

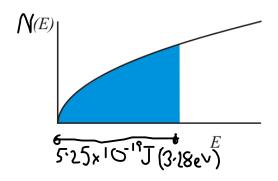
This model can be used to estimate the Fermi Energy (E<sub>F</sub>)

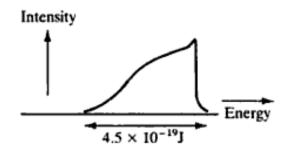
$$E_F = \frac{\hbar^2}{2m_e} \left(\frac{3\pi^2 N}{V}\right)^{2/3}$$

Where  $m_e$  = electron mass, h = plane's constant, N = number of unpaired electrons per unit volume, V = volume

e.g. for Na (1 unpaired electron per atom, lattice parameter of 4.2 Å, 2 atoms per unit cell)

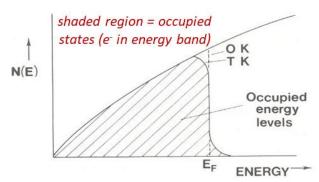
$$E_F = \frac{\hbar^2}{2m_e} \left( \frac{3\pi^2 N}{V} \right)^{2/3} = \frac{(1.0546 \times 10^{-34} \text{Js})^2}{(2 \times 9.1095 \times 10^{-31} \text{kg})} \left( \frac{3 \times 3.141592^2 \times 2}{(4.2 \times 10^{-10} \text{m})^3} \right)^{2/3}$$
$$= 5.2576 \times 10^{-19} \text{J}$$
$$= 3.28 \text{ eV}$$





Free electron density of states

Experimental x-ray emission spectroscopy



At 0 K electrons 'paired' in band orbitals (very low conductivity). The highest filled energy at 0 K is called the Fermi Energy. Above 0 K the energy with a 50% probability of occupation is called the Fermi Level (these terms are often used interchangeably which can be confusing).

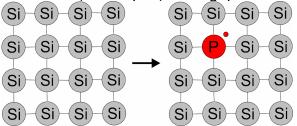
Above 0 K electrons are promoted by heat to higher energy orbitals (increases conductivity).

kT at room temperature = 4.14×10<sup>-21</sup> J (0.0258) eV Relatively few electrons are promoted into unoccupied orbitals

If there is a large N(E) more orbitals with unpaired electrons (increases conductivity) e.g. Na vs Cu

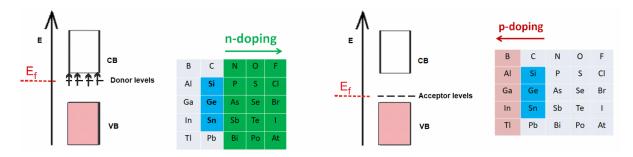
### Semiconductor Doping and Applications

Semiconductor doping modifies the conductivity and position of the Fermi level. A good example is Si which has an intrinsic (non-doped) band gap of 1.1eV.

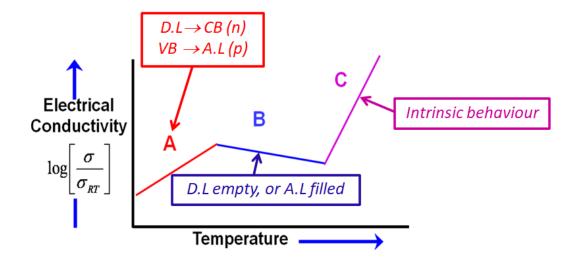


Doping with a group 15 element gives an extra electron in an orbital with an energy within the band gap (n-doping).

Doping with a group 13 element gives one fewer electron in an orbital with an energy within the band gap (p-doping).



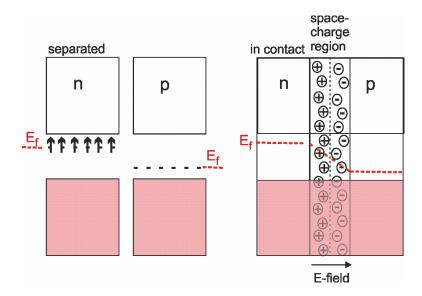
Temperature depdendent conductivity



### Fermi Levels

At the interface of **any** two substances the Fermi levels will equilibrate (electrons are transferred). This concept is the basis of all interfacial science, phenomena and reliant technology e.g. adhesion, corrosion, sensors, transistors, LED lighting + many, many more.

### Another example **p-n junction** (solar cells and LED's)



At interface of p-n junction charge is transferred (from n-p) to equilibrate the fermi levels. Charge transfer causes generation of a field in a region close to the interface (space charge region).

Solar cells (light to electricity)

Illumination of the space charge region causes excitation of an electron from the valence to conduction band.

The field separates the electron and hole inducing an electrical current.

LED's and electroluminescence (electricity to light)

Inject an electron and hole into the space charge region.

Recombination causes emission of a photon.

# Superconductivity

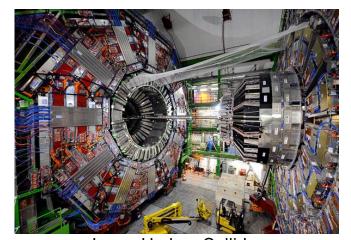
Superconductors exhibit two remarkable properties
Zero electrical resistance and the Meissner effect (an external magnetic field is ejected)

Nobel Prize (1972, 1973, 1987, 2003)





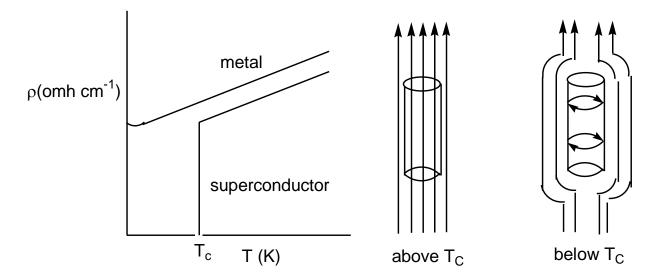
MRI NMR



Large Hadron Collider



Maglev Train



- 1. Below a critical temperature T<sub>C</sub> zero electrical resistance is observed.
- 2. Below  $T_C$  magnetic flux is expelled B = 0 (Meissner effect).  $\chi = -1$

Superconductors are used for the generation of large magnetic fields (such as NMR and MRI) because they can support very large currents without resistive heating. If the  $T_{\rm C}$  could be increased to > 300K many technologies (e.g. transport and power generation) would be revolutionised.

Superconductivity was discovered by Onnes in 1911 for Hg ( $T_C = 4.2K$ ) and many examples of superconductors have since been investigated. However until 1986 the highest known  $T_C$ 's were approximately 25K.

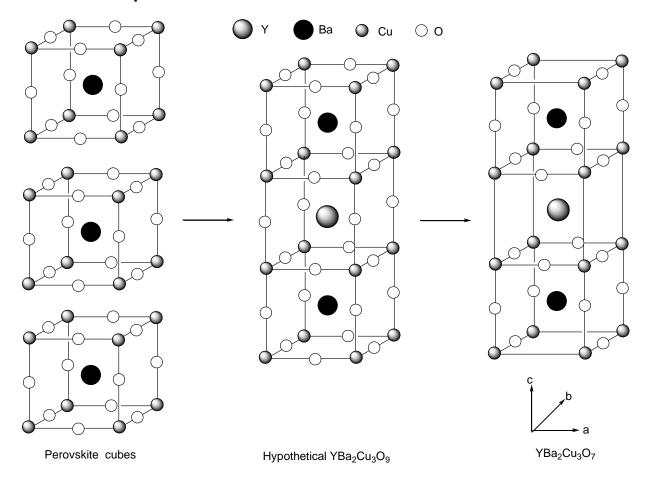
H. K. Onnes (1911). "The resistance of pure mercury at helium temperatures". *Commun. Phys. Lab. Univ. Leiden* 12: 120.

### Cuprates (high T<sub>C</sub> superconductors)

In 1986 the compound La<sub>1.8</sub>Ba<sub>0.2</sub>CuO<sub>4</sub> was reported to have a  $T_{\rm C}$  of 35K. This compound has the K<sub>2</sub>NiF<sub>4</sub> type structure that is related to the perovskites. Later the phases YBa<sub>2</sub>Cu<sub>3</sub>O<sub>7-x</sub> 0<x<1 were investigated and the T<sub>C</sub> raised to 93K. The highest T<sub>C</sub> to date is about 160K for HgBa<sub>2</sub>Ca<sub>2</sub>Cu<sub>3</sub>O<sub>10</sub> under pressure. (but there are higher claims based on hydrides)

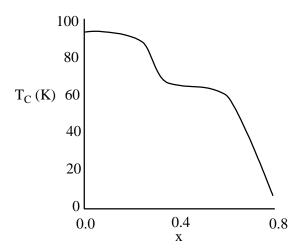
- J. G. Bednorz and K. A. Müller (1986). "Possible high T<sub>c</sub> superconductivity in the Ba-La-Cu-O system". *Z. Physik, B* **64** (1): 189–193.
- M. K. Wu et al. (1987). "Superconductivity at 93 K in a New Mixed-Phase Y-Ba-Cu-O Compound System at Ambient Pressure". *Physical Review Letters* **58** (9): 908–910.

## **Structure of Cuprates**

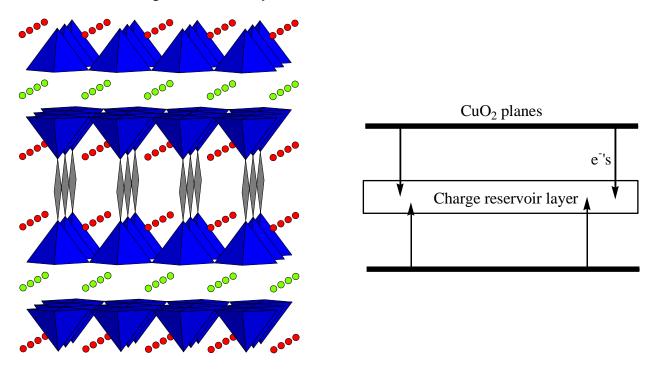


There are two copper sites: A distorted square pyramid of Jahn-teller distorted  $Cu^{2+}$  (that form  $CuO_2$  layers) and square planar geometry (that link the layers). Oxygen is removed from the basal planes  $(0, \frac{1}{2}, 0)$  for the compositions  $YBa_2Cu_3O_{7-x}$  leading to linear geometry for the Cu atoms linking the  $CuO_2$  layers. The structure is orthorhombic  $a \neq b \neq c$ .

The average oxidation state for Cu in YBa<sub>2</sub>Cu<sub>3</sub>O<sub>7-x</sub> 0<x<1 ranges from 2.33 (Cu<sup>3+</sup>/Cu<sup>2+</sup>) to 1.66 (Cu<sup>2+</sup>/Cu<sup>+</sup>).  $T_C$  is very dependent on the Cu oxidation state and hence the oxygen content. For Cu<sup>2+</sup>/Cu<sup>+</sup> YBa<sub>2</sub>Cu<sub>3</sub>O<sub>6.0-6.5</sub> antiferromagnetism is observed and superconductivity is suppressed. For Cu<sup>3+</sup>/Cu<sup>2+</sup> YBa<sub>2</sub>Cu<sub>3</sub>O<sub>6.5-7.0</sub>  $T_C$  increases with increasing oxygen content.



Studies indicate that the important structural features are  $CuO_2$  square planar layers separated by 'charge reservoir layers' that control the average Cu oxidation state in the  $CuO_2$  layers. The average Cu oxidation state should also be > 2+. For  $YBa_2Cu_3O_7$  the charge reservoir layers are CuO chains.

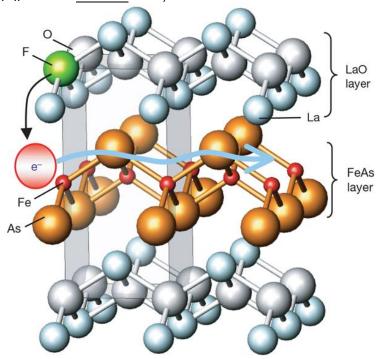


### **FeAs**

2008 a new family of superconductors based on FeAs layers separated by LaO layers. cf. the structure of cuprates.

e.g. LaO<sub>1-x</sub>F<sub>x</sub>FeAs

Hideo Hosono et al (2008). "Superconductivity at 43 K in an iron-based layered compound LaO<sub>1-x</sub>F<sub>x</sub>FeAs". *Nature* **453**, 376.

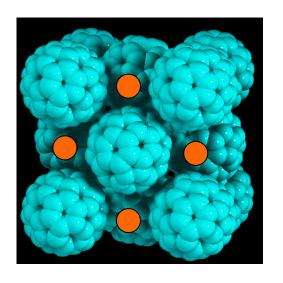


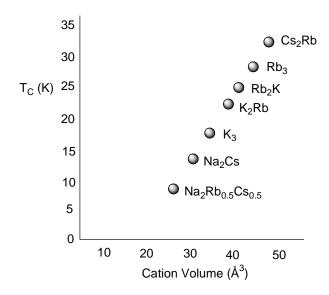
#### **Fullerides**

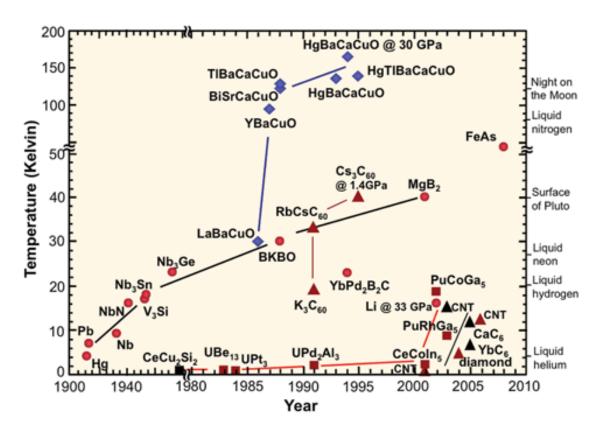
Synthesised by intercalation of electropositive metals into the C<sub>60</sub> lattice.

Electron transfer from the metal to  $C_{60}$  gives  $C_{60}^{n-}$  anions (fullerides). The orbitals of neighbouring  $C_{60}$  molecules overlap forming bands and the electrons are able to move throughout the solid i.e metallic.  $T_C$  high for molecular based solid.

For the superconducting  $A_3C_{60}$  (A = alkali metal) that have a cubic structure, all the tetrahedral and octahedral interstitial sites are filled.  $T_C$  is proportional to the average cation volume (the distance between  $C_{60}$  molecules).







## Theory of superconductivity (conventional superconductivity)

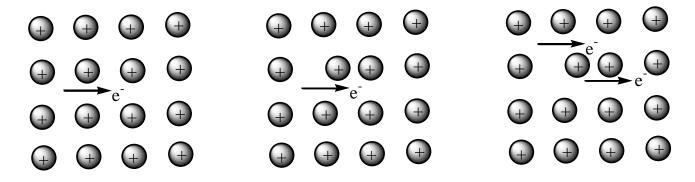
J. Bardeen, L. N. Cooper and J. R. Schrieffer (1957). "Microscopic Theory of Superconductivity". *Physical Review* **106** (1): 162–164.

The theory(ies) of superconductivity are mathematically very complicated however a qualitative picture of one (BCS theory) can be given.

BCS (Bardeen, Cooper, and Schrieffer) theory describes the mutual attraction of two conduction electrons mediated by lattice vibrations.

In the same way electromagnetic waves can be quantised as photons, the frequencies of lattice vibrations can also be quantised as *phonons*. Electron-phonon coupling is the mechanism by which electrons can be attracted to each other. The two electrons are known collectively as a *Cooper pair*.

The two electrons do not have to be close to each other and can be many thousands of atomic spacings apart.



Electron-phonon coupling

The importance of phonons can be demonstrated experimentally by the use of isotopes.  $T_C$  is inversely proportional to  $\sqrt{M}$  where M is the mass of a lattice ion.

Except for at very low temperatures the resistance of metals is due to the scattering of electrons by phonons, which is one reason why the resistance of metals increases with increasing temperature. (more phonons at higher temperature). For superconductors Cooper pairs are not scattered and therefore have zero resistance.

There is of course a repulsive electrostatic interaction between two electrons. Electron-phonon coupling must be strong for the Copper pair to remain intact and it must be greater than electron-electron repulsion. The binding energy of Cooper pairs is usually weak and this is why  $T_{\rm C}$  is usually low.

#### **Nanomaterials**

Have been known for millennia but have hit the headlines more recently because of their remarkable properties and the development of synthetic and analytical tools to characterise and manipulate them. (mainly metals and metal oxides, but more recently carbon based e.g. carbon nanotubes and graphene)

Many properties have size dependence. Nanomaterials are focused mainly on structures with a dimension between 1 - 100 nm, bridging the gap between molecules (0.1 - 10 nm) and traditional solid state compounds > 100 nm.

## **Size Dependent Properties**

e.g.

Optical
Magnetic
Electronic
Catalytic
Mechanical

## **Nanotechnology Applications**

## **Technological**

Colour (colloids, quantum dots)

Computing (Magnetic memory, spintronics)

Strong and dense materials (reduce brittleness and fatigue)

Catalysis (Car converters, fuel cells, chemicals)

Energy Conversion (solar, electromechanical)

### Health

Imaging (microscopy, MRI)

Drug Delivery (needleless injection)

Magnetic heating (anti-cancer)

Protection (sunscreen)

### **Food**

Additives

## **Nanoparticles**

How many atoms are in e.g. a 2 nm diameter silver nanoparticle? Assume a sphere, Ag atom radius = 172 pm

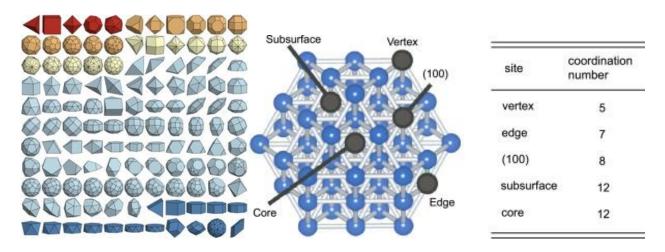
$$V_{Ag} = \frac{4\pi r^3}{3} = 0.0213 \text{ nm}^3$$

$$V_{np} = 4.18 \text{ nm}^3$$

i.e. A lot of the nanoparticle atoms will be at the surface.

## **Shapes of nanoparticles**

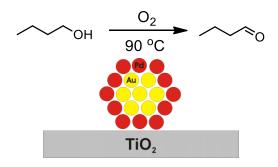
But nanoparticles are not spherical. Exhibit a range of shapes. Each shape and surface has unique energy and electronic structure. Certain shapes preferred thermodynamically. Surface can have many defects.



Cubeoctahedron is very common shape. Surfaces with low miller indices generally have lower surface energy. All this leads to chemistry that may be very different from the bulk material and is sensitive to the surface structure and number and type of defects. e.g. in catalysis and sensing.

e.g. gold is generally considered inert, but as nanoparticles it is a good oxidation catalyst. When mixed with other metals, alloys are formed.

2.5% Au/Pd supported on TiO<sub>2</sub>. No stoichiometric oxidant required (Cr, Mn, peroxides etc). Oxidation with air at low T. Alloy nanoparticle is core shell Au@Pd.



### How can shape be controlled?

### Wet chemical methods

Used to prepare soluble nanoparticles. Need to prevent aggregation which causes precipitation. Need to coat the nanoparticle surface.

Ligands can form a steric barrier or cause electrostatic repulsion between particles. Steric barrier most common. Can use many long chain 'fatty' acids, amines, thiols, phosphines which covalently bind to the metal or metal compound surface.

### e.g. Reduction of metal salts or compounds to make metal nanoparticles

Electrostatic stabilisation of the gold. The ammonium ions are not covalently bound to the metal surface. Can add thiols to bind strongly and increase stabilisation.

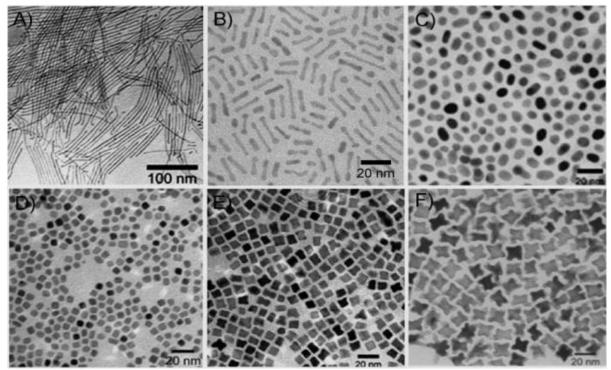
Metal oxides and other semiconductors prepared by hydrolysis or decomposition of a metal compound or complex in the presence of a ligand that binds covalently to the surface.

e.g. 
$$CdO + Se + P(C_8H_{17})_3 \longrightarrow CdSe_{np} + byproducts$$
 
$$Ti(OiPr)_4 + 2 H_2O + C_{18}H_{33}CO_2H \longrightarrow TiO_{2 np} + 4 iPrOH$$
 oleic acid

Size and shape of the nanoparticles can be controlled by synthesis temperature, time and relative concentrations of ligand and metal precursor.

### e.g. FePt nanocrystals

$$\begin{array}{c} C_{18}H_{33}CO_{2}H\\ \text{oleic acid} \\ \\ \text{Pt(acac)}_{2}+ & \text{Fe(CO)}_{5} + \frac{C_{18}H_{35}NH_{2}}{\text{oleylamine}} & \xrightarrow{300~^{\circ}\text{C}} \\ \\ C_{14}H_{29}CH(OH)CH_{2}(OH)\\ \\ 1,2-\text{hexadecanediol} \end{array} \qquad \begin{array}{c} \text{PtFe} \\ \text{P$$



FePt nanocrystals Narayan Poudyal, J. Appl. Phys. 2009, 105, 07A749

Varying the ligand concentrations and temperature changes the shape. The ligands will bind preferentially to specific surfaces (e.g. 001) and prevent growth in this direction.

Solubility allows use in solution chemistry (e.g. biological applications) and processing to make materials containing isolated nanoparticles e.g. for catalysis.

## **Characterisation of Nanoparticles**

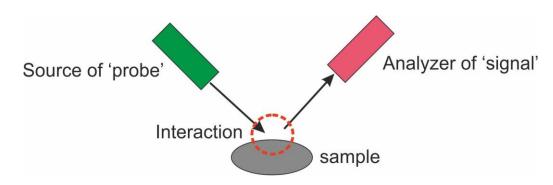
Development of analytical tools has revolutionized materials (nano)science

#### What would we like to know?

#### These include

- 1. Composition: stoichiometry(elemental analysis) and particle homogeneity
- 2. Structure: internal bulk, surface, defects
- 3. Morphology and particle size: shape and size distribution of particles
- 4. Properties (e.g. magnetic, electrical, dielectric, optical, catalytic, dynamic)

### **Analysis**



Probe: photons, electrons, neutrons, ions

Interaction: absorption, absorption-emission, reflection, refraction, diffraction, scattering.

Signal: photons, electrons, neutrons, ions

Can perform measurements as a function of time, temperature, pressure, and field (electric and magnetic).

#### Considerations

- 1. Probe size (spatial resolution). Is the probe 'local' with high spatial resolution or will the signal be averaged over a larger interaction volume.
- 2. Timescale (temporal resolution). Are the timescales of the source and analyser fast compared to the phenomenon of interest.

### Common analytical techniques for structure and composition

Diffraction Methods: Single crystal if lucky but often powders.

X-ray Diffraction (Nobel Prize 1914, 1915, 1985): Maps electron density giving the relative atomic positions.

Neutron Diffraction (Nobel Prize 1994): Based on scattering length and cross section of individual isotopes (not related to electron density e.g <sup>2</sup>H gives large response). Neutrons also have a magnetic moment allowing the magnetic structure to be determined.

Electron Diffraction (Nobel Prize 1937). Most often used in conjunction with electron microscopy (see below). Sensitive to electron density similar to x-ray diffraction. Can be used on individual nanocrystals.

Note that the structures obtained are an average structure.

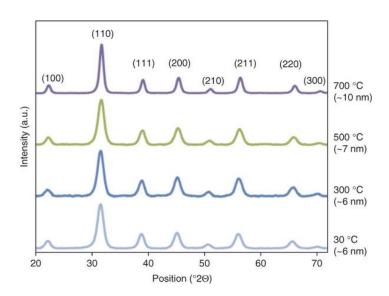
## Particle Size from X-ray Diffraction

The width of diffraction peaks increase as the size decreases and is described by the Scherrer equation. Applicable to particles <100 nm.

$$\tau = \frac{\kappa\lambda}{\beta cos\theta}$$

Where  $\tau$  = particle size,  $\kappa$  = shape factor,  $\lambda$  = x-ray wavelength,  $\beta$  = full width half maximum (fwhm) in radians (1 degree =  $\pi/180$  radians),  $\theta$  = Bragg angle.

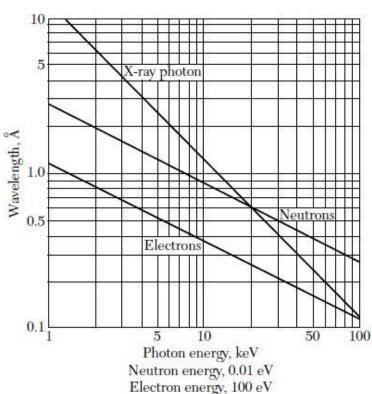
e.g. BaTiO<sub>3</sub> nanoparticles. Synthesised at 500 °C, the 111 reflection measured using Cu X-rays (1.5418 Å), at 39.45° 2 $\theta$ , has a fwhm of 1.20° (0.0210 radians). Assume a shape factor of 0.9,  $\tau$  = 7 nm.



The calculated value does not include other effects of broadening so is often an underestimation.

For BiTiO<sub>3</sub> the particles are growing (sintering) with heating because larger particles have lower surface area and hence surface energy.

**Electron microscopy and scanning probe microscopy** (Nobel Prize 1928, 1929, 1986)



Why do we need electron microscopy?

Two distinguish two positions you need sufficient resolving power For standard optics the minimum distance that can be resolved is described by The Abbe diffraction limit.

$$d = \frac{\lambda}{2n \sin \theta}$$

Where d (minimum resolvable distance),  $\lambda$  (wavelength), n (refractive index),  $\theta$  (half angle light is converging to).

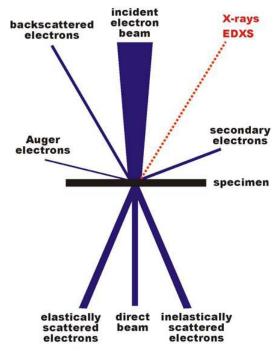
Shorter wavelength = smaller distance that can be resolved.

Wave-particle duality. All moving matter has wave properties.

$$\frac{\lambda = h/p}{h} = \frac{h}{mv}$$
(h = Planck constant;  $p = momentum$ ; m = mass; v = velocity)

Therefore a high energy collimated electron beam can be used to image very small distances

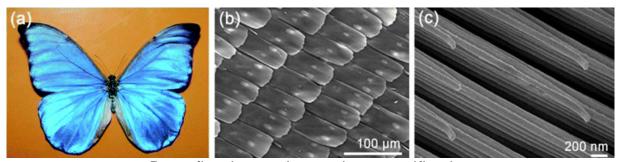
Electron Microscopy: Usually performed in vacuum to reduce electron scattering



Electron beams can interact (elastically and inelastically) with solids in many ways, which can be used to probe the structure and properties of materials. Needs fancy electron 'optics' to focus the beam =  $\pounds\pounds$ .

SEM (scanning electron microscopy): Back scattered and secondary electrons give morphology and particle size distribution. Resolution 10 nm -10  $\mu$ m.

Energy Dispersive Spectroscopy (EDS, EDXS, EDX): Used with SEM. Electrons used to excite inner electrons of atoms and then emit a characteristic photon giving an element map.



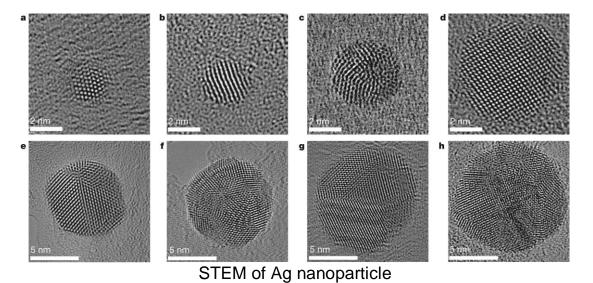
Butterfly wings at increasing magnification

TEM and STEM ((scanning) transmission electron microscopy): requires thin sample so electrons pass through and uses scattered electrons to image. Resolution Atomic - 100 nm. Also usually fitted with EDS

### Other modes:

Electron diffraction also gives information about the crystal structure of individual particles including defects.

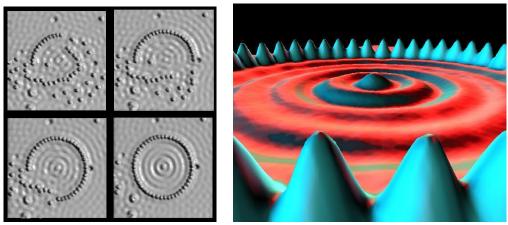
Electron energy loss spectroscopy (EELS): Similar in principle to EDS but better for lighter elements and can probe valence electrons and chemical bonding. Can generate element maps with atomic resolution.



Scanning probe microscopy (SPM): Used in vacuum or in liquids

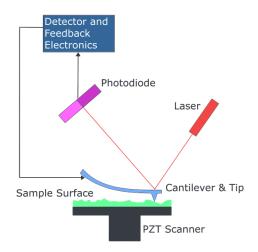
Used for surface characterisation to map structure but also function (e.g. magnetic and electrical properties)

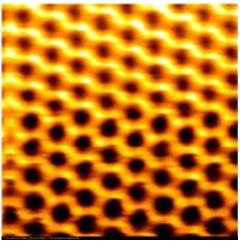
STM (scanning tunnelling microscopy): Atomic resolution imaging and atom manipulation. Uses piezoelectric crystals to maintain a current between the tip and sample.



Quantum corral 'particle in a box'

Atomic Force Microscopy (AFM): Measures deflection of a tip as it is scanned across the surface of a material. Sub nm resolution now possible. Can be used for direct imaging but also many other functional modes (e.g. electrochemistry).





AFM of graphite

## Other common spectroscopic techniques

### **Using electrons**

X-ray fluorescence spectroscopy (XRF) (Nobel Prize 1924): Quick method to determine elemental analysis of a solid. Very similar to EDS and EELS but at much lower resolution (µm-mm)

X-ray photoelectron spectroscopy (XPS) (Nobel Prize 1981): surface composition and oxidation states

## **Using photons**

Solid state NMR spectroscopy: Local structure and dynamics (need active nuclei)

Electron spin resonance (EPR): Local structure and defects

Uv-Vis spectroscopy: Band gap of semiconductors Raman spectroscopy: Vibrations (phonons) in crystals

Summary

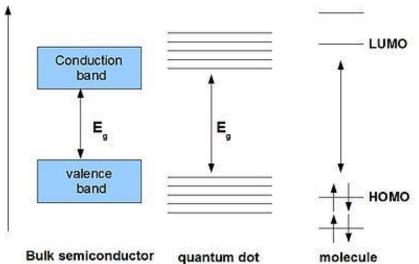
_	X-ray/Neut. diffraction	SEM	TEM	STM	AFM	NMR and ESR	XPS
Bulk elemental composition	X	Х	X				
Crystal structure	X		Х				
Local structure	X		х			х	
Defects			Х			Х	
Morphology		Х	Х				
Surface structure				Х	Х		
Surface composition				Х	Х		Х
Oxidation state			X				X

## **Electronic structure and Optical properties of Nanoparticles**

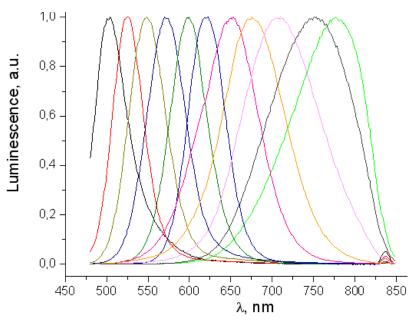
Differences between metals and semiconductors.

#### Semiconductors

As the number of atoms and size reduces the band structure tends toward that of a molecule.



When a photon is absorbed an exited state (electron-hole pair) called an exciton is generated. Relaxation can lead to luminescence (fluorescence) which is size dependent. Nanoparticles in this size regime are called quantum dots. The band gap (Eg) will increase with decreasing size.



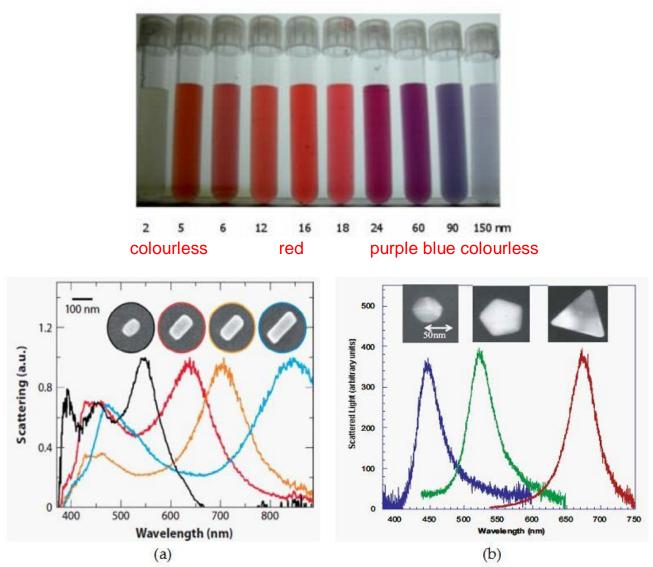
CdTe nanoparticles fluoresce in the visible region (size increases left to right).

Can be used as sensors and tags in biology (more inert than organic dyes). Solar energy conversion. Light emitting diodes.

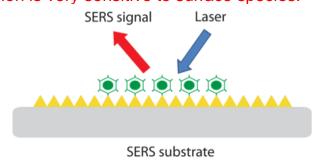
### **Metals**

In metals the conduction band is retained until very small particle size (ca. 2 nm). The conduction electrons can absorb light leading to a collective excitation. This excitation is called Surface Plasmon Resonance (SPR). For some metals SPR is in the visible region (gold, silver and copper) leading to colour. The SPR is dependent on a number of factors including size and shape.

e.g. gold nanoparticles have size and shape dependent colours.



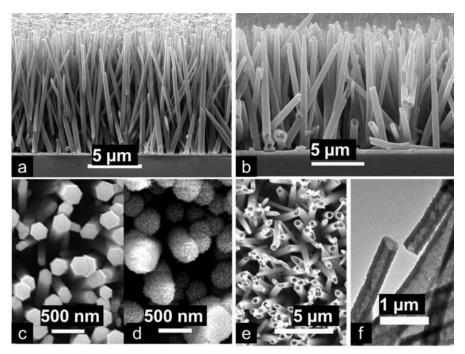
Used for centuries to stain glass, also more recently in medicine, but most commonly now in very sensitive sensors (surface enhanced Raman spectroscopy (SERS)) as the plasmon is very sensitive to surface species.



### Other uses of nanostructured materials

### **Nanotubes**

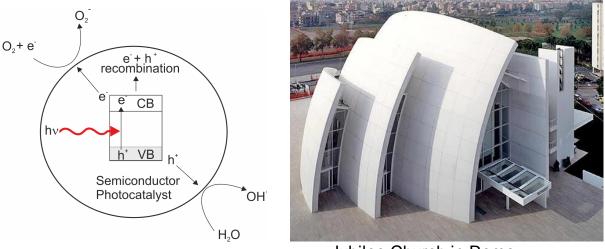
e.g. TiO<sub>2</sub> nanotubes formed electrochemically by etching Ti metal foil with HF.



Nanotube structure changes the surface energy preventing wetting, which reduces the growth of bacteria. Used as antibacterial surfaces e.g. for metal surgical implants.

### **Photocatalysts**

e.g. TiO<sub>2</sub> nanoparticles

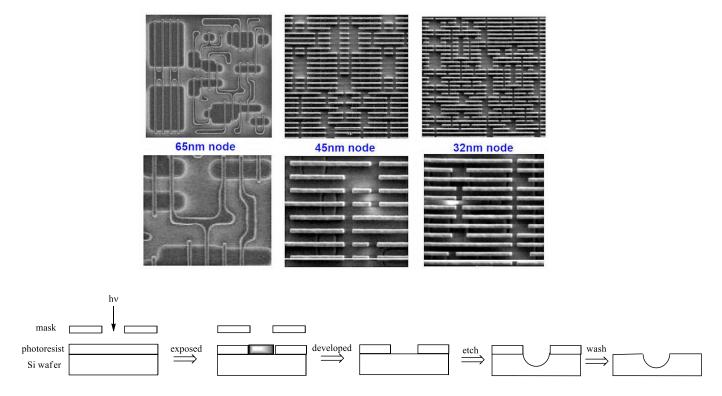


Jubilee Church in Rome

OH and O<sub>2</sub> are strong oxidizing agents and will degrade organic compounds to CO<sub>2</sub> and H<sub>2</sub>O. TiO<sub>2</sub> (titania) is used to clean surfaces, reduce air pollution and clean drinking water. Can add to materials including plastics, glasses and concrete.

## Integrated circuits

Based on silicon with <100 nm features are prepared using photolithography.



The size of the features largely determines the computing power. The photoresist is usually a polysilane. The etching step can be an acid or usually a plasma. Can also add dopants onto the exposed wafer.

Current state-of-the-art 10 nm feature size (25 million transistors per mm<sup>2</sup>)

### **Additives**

One of the biggest markets for inorganic (nano)materials are in additives used for a very wide range of products including coatings (e.g. paint) for protection and colour. Some applications are in direct contact with humans including food, cosmetics and suncreams. *Environ. Sci.: Nano*, **2019**, 6, 1549.

e.g. TiO<sub>2</sub> (E171) used to whiten sweets, ice-cream, icing, chewing gum, bread, pastries + lots of other products.

Current controversy over safety and some countries have recently banned its use.

## A selection of other food additives and their uses

Colours					
E171	Titanium Dioxide	White			
E172	Iron oxides and iron hydroxides	Brown			
E173	Aluminium	Silver/Grey			
E174	Silver	Silver			
E175	Gold	Gold			
Additives					
E518	Magnesium sulfate (Epsom salts), (acidity regulator)	firming agent			
E519	Copper(II) sulfate	preservative			
E520	Aluminium sulfate	firming agent			
E521	Aluminium sodium sulfate	firming agent			
E522	Aluminium potassium sulfate	acidity regulator			
E523	Aluminium ammonium sulfate	acidity regulator			
E524	Sodium hydroxide	acidity regulator			
E525	Potassium hydroxide	acidity regulator			
E526	Calcium hydroxide (acidity regulator)	firming agent			
E527	Ammonium hydroxide	acidity regulator			
E528	Magnesium hydroxide	acidity regulator			
E529	Calcium oxide (acidity regulator)	improving agent			
E530	Magnesium oxide (acidity regulator)	anti-caking agent			
E535	Sodium ferrocyanide (acidity regulator)	anti-caking agent			
E536	Potassium ferrocyanide	anti-caking agent			
E537	Ferrous hexacyanomanganate	anti-caking agent			
E538	Calcium ferrocyanide	anti-caking agent			
E539	Sodium thiosulfate	antioxidant			
E540	Dicalcium diphosphate[citation needed] (acidity regulator)	emulsifier			
E541	Sodium aluminium phosphate (i) Acidic (ii) Basic	emulsifier			
E542	Bone phosphate (Essentiale Calcium Phosphate, Tribasic)	anti-caking agent			
E543	Calcium sodium polyphosphate	emulsifier			
E544	Calcium polyphosphate	emulsifier			
E545	Ammonium polyphosphate	emulsifier			
E550	Sodium Silicates (i) Sodium silicate (ii) Sodium metasilicate	anti-caking agent			
E551	Silicon dioxide (Silica)	anti-caking agent			
E552	Calcium silicate	anti-caking agent			
E553a	(i) Magnesium silicate (ii) Magnesium trisilicate	anti-caking agent			
E553b	Talc	anti-caking agent			
E560	Potassium silicate	anti-caking agent			