

## AUGUSTUS DE MORGAN\*

(1806–1871)

AUGUSTUS DE MORGAN was born in the month of June at Madura in the presidency of Madras, India; and the year of his birth may be found by solving a conundrum proposed by himself, “I was  $x$  years of age in the year  $x^2$ .” The problem is indeterminate, but it is made strictly determinate by the century of its utterance and the limit to a man’s life. His father was Col. De Morgan, who held various appointments in the service of the East India Company. His mother was descended from James Dodson, who computed a table of anti-logarithms, that is, the numbers corresponding to exact logarithms. It was the time of the Sepoy rebellion in India, and Col. De Morgan removed his family to England when Augustus was seven months old. As his father and grandfather had both been born in India, De Morgan used to say that he was neither English, nor Scottish, nor Irish, but a Briton “unattached,” using the technical term applied to an undergraduate of Oxford or Cambridge who is not a member of any one of the Colleges.

When De Morgan was ten years old, his father died. Mrs. De Morgan resided at various places in the southwest of England, and her son received his elementary education at various schools of no great account. His mathematical talents were unnoticed till he had reached the age of fourteen. A friend of the family accidentally discovered him making an elaborate drawing of a figure in Euclid with ruler and compasses, and explained to him the aim of Euclid, and gave him an initiation into demonstration.

De Morgan suffered from a physical defect—one of his eyes was rudimentary and useless. As a consequence, he did not join in the sports of the other boys, and he was even made the victim of cruel practical jokes by some schoolfellows. Some psychologists have held that the perception of distance and of solidity depends on the action of two eyes, but De Morgan testified that so far as he could make out he perceived with his one eye distance and solidity just like other people.

He received his secondary education from Mr. Parsons, a Fellow of Oriel College, Oxford, who could appreciate classics much better than mathematics. His mother was an active and ardent member of the Church of England, and desired that her son should become a clergyman; but by this time De Morgan had begun to show his non-grooving disposition, due no doubt to some extent to his physical infirmity. At the age of sixteen he was entered at Trinity College Cambridge, where he immediately came under the tutorial influence of Peacock and Whewell. They became his life-long friends; from the former he derived an interest in the renovation of algebra, and from the latter an interest in the renovation of logic—the two subjects of his future life work.

At college the flute, on which he played exquisitely, was his recreation. He took no part in athletics but was prominent in the musical clubs. His love of knowledge for its own sake interfered with training for the great mathematical race; as a consequence he came out fourth wrangler. This entitled him to the degree of Bachelor of Arts; but to take the higher degree of Master of Arts and thereby become eligible for a fellowship it was then necessary to pass a theological test. To the signing of any such test De Morgan felt a strong objection, although he had been brought up in the Church of

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England. About 1875 theological tests for academic degrees were abolished in the Universities of Oxford and Cambridge.

As no career was open to him at his own university, he decided to go to the Bar, and took up residence in London; but he much preferred teaching mathematics to reading law. About this time the movement for founding, the London University took shape. The two ancient universities were so guarded by theological tests that no Jew or Dissenter from the Church of England could enter as a student; still less be appointed to any office. A body of liberal-minded men resolved meet the difficulty by establishing in London a University on the principle of religious neutrality. De Morgan, then 22 years of age, was appointed Professor of Mathematics. His introductory lecture "On the study of mathematics" is a discourse upon mental education of permanent value—which has been recently reprinted in the United States.'

The London University was a new institution, and the relations of the Council of management, the Senate of professors and the body of students were not well defined. A dispute arose between the professor of anatomy and his students, and in consequence of the action taken by the Council, several of the professors resigned, headed by De Morgan. Another professor of mathematics was appointed, who was accidentally drowned a few years later. De Morgan had shown himself a prince of teachers: he was invited to return to his chair, which thereafter became the continuous center of his labors for thirty years.

The same body of reformers—headed by Lord Brougham, a Scotsman eminent both in science and politics—who had instituted the London University, founded about the same time a Society for the Diffusion of Useful Knowledge. Its object was to spread scientific and other knowledge by means of cheap and clearly written treatises by the best writers of the time. One of its most voluminous and effective writers was De Morgan. He wrote a great work on *The Differential and Integral Calculus* which was published by the Society; and he wrote one-sixth of the articles in the *Penny Cyclopaedia*, published by the Society, and issued in penny numbers. When De Morgan came to reside in London he found a congenial friend in William Frennd, notwithstanding his mathematical heresy about negative quantities. Both were arithmeticians and actuaries, and their religious views were somewhat similar. Frennd lived in what was then a suburb of London, in a country-house formerly occupied by Daniel Defoe and Isaac Watts. De Morgan with his flute was a welcome visitor; and in 1837 he married Sophia Elizabeth, one of Frennd's daughters.

The London University of which De Morgan was a professor was a different institution from the University of London. The University of London was founded about ten years later by the Government for the purpose of granting degrees after examination, without any qualification as to residence. The London University was affiliated as a teaching college with the University of London, and its name was changed to University College. The University of London was not a success as an examining body; a teaching University was demanded. De Morgan was a highly successful teacher of mathematics. It was his plan to lecture for an hour, and at the close of each lecture to give out a number of problems and examples illustrative of the subject lectured on; his students were required to sit down to them and bring him the results, which he looked over and returned revised before the next lecture. In De Morgan's opinion, a thorough comprehension and mental assimilation of great principles far outweighed in import-

ance any merely analytical dexterity in the application of half-understood principles to particular cases.

De Morgan had a son George, who acquired great distinction in mathematics both at University College and the University of London. He and another like-minded alumnus conceived the idea of founding a Mathematical Society in London, where mathematical papers would be not only received (as by the Royal Society) but actually read and discussed. The first meeting was held in University College; De Morgan was the first president, his son the first secretary. It was the beginning of the London Mathematical Society. In the year 1866 the chair of mental philosophy in University College fell vacant. Dr. Martineau, a Unitarian clergyman and professor of mental philosophy, was recommended formally by the Senate to the Council; but in the Council there were some who objected to a Unitarian clergyman, and others who objected to theistic philosophy. A layman of the school of Bain and Spencer was appointed. De Morgan considered that the old standard of religious neutrality had been hauled down, and forthwith resigned. He was now 60 years of age. His pupils secured a pension of \$500 for him, but misfortunes followed. Two years later his son George—the younger Bernoulli, as he loved to hear him called, in allusion to the two eminent mathematicians of that name, related as father and son—died. This blow was followed by the death of a daughter. Five years after his resignation from University College De Morgan died of nervous prostration on March 18, 1871, in the 65th year of his age.

De Morgan was a brilliant and witty writer, whether as a controversialist or as a correspondent. In his time there flourished two Sir William Hamiltons who have often been confounded. The one Sir William was a baronet (that is, inherited the title), a Scotsman, professor of logic and metaphysics in the University of Edinburgh; the other was a knight (that is won the title), an Irishman, professor of astronomy in the University of Dublin. The baronet contributed to logic the doctrine of the quantification of the predicate; the knight, whose full name was William Rowan Hamilton contributed to mathematics the geometric algebra called Quaternions. De Morgan was interested in the work of both, and corresponded with both; but the correspondence with the Scotsman ended in a public controversy, whereas that with the Irishman was marked by friendship and terminated only by death. In one of his letters to Rowan, De Morgan says, “Be it known unto you that I have discovered that you and the other Sir W. H. are reciprocal polars with respect to me (intellectually and morally, for the Scottish baronet is a polar bear, and you, I was going to say, are a polar gentleman). When I send a bit of investigation to Edinburgh, the W. H. of that ilk says I took it from him. When I send you one, you take it from me, generalize it at a glance, bestow it thus generalized upon society at large, and make me the second discoverer of a known theorem.”

The correspondence of De Morgan with Hamilton the mathematician extended over twenty-four years; it contains discussions not only of mathematical matters, but also of subjects of general interest. It is marked by geniality on the part of Hamilton and by wit on the part of De Morgan. The following is a specimen: Hamilton wrote, “My copy of Berkeley’s work is not mine; like Berkeley, you know, I am an Irishman.” De Morgan replied, “Your phrase ‘my copy is not mine’ is not a bull. It is perfectly good English to use the same word in two different senses in one sentence, particularly when there is usage. Incongruity of language is no bull, for it expresses meaning. But incongruity of ideas (as in the case of the Irishman who was pulling up the rope, and finding it did

not finish, cried out that somebody had cut of the other end of it) is the genuine bull.”

De Morgan was full of personal peculiarities. We have noticed his almost morbid attitude towards religion, and the readiness with which he would resign an office. On the occasion of the installation of his friend, Lord Brougham, as Rector of the University of Edinburgh, the Senate offered to confer on him the honorary degree of LL.D.; he declined the honor as a misnomer. He once printed his name: Augustus De Morgan,

H·O·M·O · P·A·U·C·A·R·U·M · L·I·T·E·R·A·R·U·M.

He disliked the country, and while his family enjoyed the sea-side, and men of science were having a good time at a meeting of the British Association in the country he remained in the hot and dusty libraries of the metropolis. He said that he felt like Socrates, who declared that the farther he got from Athens the farther was he from happiness. He never sought to become a Fellow of the Royal Society, and he never attended a meeting of the Society; he said that he had no ideas or sympathies in common with the physical philosopher. His attitude was doubtless due to his physical infirmity, which prevented him from being either an observer or an experimenter. He never voted at an election, and he never visited the House of Commons, or the Tower, or Westminster Abbey.

Were the writings of De Morgan published in the form of collected works, they would form a small library. We have noticed his writings for the Useful Knowledge Society. Mainly through the efforts of Peacock and Whewell, a Philosophical Society had been inaugurated at Cambridge; and to its Transactions De Morgan contributed four memoirs on the foundations of algebra, and an equal number on formal logic. The best presentation of his view of algebra is found in a volume, entitled *Trigonometry and Double Algebra*, published in 1849; and his earlier view of formal logic is found in a volume published in 1847. His most unique work is styled a *Budget of Paradoxes*; it originally appeared as letters in the columns of the *Athenæum* journal; it was revised and extended by De Morgan in the last years of his life, and was published posthumously by his widow. “If you wish to read something entertaining,” said Professor Tait to me, “get De Morgan’s *Budget of Paradoxes* out of the library.” We shall consider more at length his theory of algebra, his contribution to exact logic, and his Budget of Paradoxes.

In my last lecture I explained Peacock’s theory of algebra. It was much improved by D. F. Gregory, a younger member of the Cambridge School, who laid stress not on the permanence of equivalent forms, but on the permanence of certain formal laws. This new theory of algebra as the science of symbols and of their laws of combination was carried to its logical issue by De Morgan; and his doctrine on the subject is still followed by English algebraists in general. Thus Chrystal founds his *Textbook of Algebra* on De Morgan’s theory; although an attentive reader may remark that he practically abandons it when he takes up the subject of infinite series. De Morgan’s theory is stated in his volume on *Trigonometry and Double Algebra*. In the chapter (of the book) headed “On symbolic algebra” he writes: “In abandoning the meaning of symbols, we also abandon those of the words which describe them. Thus addition is to be, for the present, a sound void of sense. It is a mode of combination represented by +; when + receives its meaning, so also will the word addition. It is most important

that the student should bear in mind that, *with one exception*, no word nor sign of arithmetic or algebra has one atom of meaning throughout this chapter, the object of which is symbols, and their laws of combination, giving a symbolic algebra which may hereafter become the grammar of a hundred distinct significant algebras. If any one were to assert that + and – might mean reward and punishment, and  $A, B, C$ , etc., might stand for virtues and vices, the reader might believe him, or contradict him, as he pleases, but not out of this chapter. The one exception above noted, which has some share of meaning, is the sign = placed between two symbols as in  $A = B$ . It indicates that the two symbols have the same resulting meaning, by whatever steps attained. That  $A$  and  $B$ , if quantities, are the same amount of quantity; that if operations, they are of the same effect, etc.”

Here it may be asked, why does the symbol prove refractory to the symbolic theory? De Morgan admits that there is one exception; but an exception proves the rule, not in the usual but illogical sense of establishing it, but in the old and logical sense of testing its validity. If an exception can be established, the rule must fall, or at least must be modified. Here I am talking not of grammatical rules, but of the rules of science or nature.

De Morgan proceeds to give an inventory of the fundamental symbols of algebra, and also an inventory of the laws of algebra. The symbols are 0, 1, +, –, ×, ÷,  $()^0$  and letters; these only, all others are derived. His inventory of the fundamental laws is expressed under fourteen heads, but some of them are merely definitions. The laws proper may be reduced to the, following, which, as he admits, are not all independent of one another:

- I. Law of signs.  $++ = +, +- = -, -+ = -, -- = +, \times \times = \times, \times \div = \div, \div \times = \div, \div \div = \times.$
- II. Commutative law.  $a + b = b + a, ab = ba.$
- III. Distributive law.  $a(b + c) = ab + ac.$
- IV. Index laws.  $a^b \times a^c = a^{b+c}, (a^b)^c = a^{bc}, (ab)^c = a^c b^c$
- V.  $a - a = 0, a \div a = 1.$

The last two may be called the rules of reduction. De Morgan professes to give a complete inventory of the laws which the symbols of algebra must obey, for he says, “Any system of symbols which obeys these laws and no others, except they be formed by combination of these laws, and which uses the preceding symbols and no others, except they be new symbols invented in abbreviation of combinations of these symbols, is symbolic algebra.” From his point of view, none of the above principles are rules; they are formal laws, that is, arbitrarily chosen relations to which the algebraic symbols must be subject. He does not mention the law, which had already been pointed out by Gregory, namely,  $(a + b) + c = a + (b + c), (ab)c = a(bc)$  and to which was afterwards given the name of the law of association. If the commutative law fails, the associative may hold good; but not *vice versa*. It is an unfortunate thing for the symbolist or formalist that in universal arithmetic  $m^n$  is not equal to  $n^m$ ; for then the commutative law would have full scope. Why does he not give it full scope? Because the foundations

of algebra are, after all, real not formal, material not symbolic. To the formalists the index operations are exceedingly refractory, in consequence of which some take no account of them, but relegate them to applied mathematics. To give an inventory of the laws which the symbols of algebra must obey is an impossible task, and reminds one not a little of the task of those philosophers who attempt to give an inventory of the *a priori* knowledge of the mind.

De Morgan's work entitled *Trigonometry and Double Algebra* consists of two parts; the former of which is a treatise on Trigonometry, and the latter a treatise on generalized algebra which he calls Double Algebra. But what is meant by Double as applied to algebra? and why should Trigonometry be also treated in the same textbook? The first stage in the development of algebra is *arithmetic*, where numbers only appear and symbols of operations such as +, ×, etc. The next stage is *universal arithmetic*, where letters appear instead of numbers, so as to denote numbers universally, and the processes are conducted without knowing the values of the symbols. Let  $a$  and  $b$  denote any numbers; then such an expression as  $a - b$  may be impossible; so that in universal arithmetic there is always a proviso, *provided the operation is possible*. The third stage is *single algebra*, where the symbol may denote a quantity forwards or a quantity backwards, and is adequately represented by segments on a straight line passing through an origin. Negative quantities are then no longer impossible; they are represented by the backward segment. But an impossibility still remains in the latter part of such an expression as  $a + b\sqrt{-1}$  which arises in the solution of the quadratic equation. The fourth stage is *double algebra*; the algebraic symbol denotes in general a segment of a line in a given plane; it is a double symbol because it involves two specifications, namely, length and direction; and  $\sqrt{-1}$  is interpreted as denoting a quadrant. The expression  $a + b\sqrt{-1}$  then represents a line in the plane having an abscissa  $a$  and an ordinate  $b$ . Argand and Warren carried double algebra so far; but they were unable to interpret on this theory such an expression as  $e^{a\sqrt{-1}}$ . De Morgan attempted it by reducing such an expression to the form  $b + q\sqrt{-1}$ , and he considered that he had shown that it could be always so reduced. The remarkable fact is that this double algebra satisfies all the fundamental laws above enumerated, and as every apparently impossible combination of symbols has been interpreted it looks like the complete form of algebra.

If the above theory is true, the next stage of development ought to be *triple algebra* and if  $a + b\sqrt{-1}$  truly represents a line in a given plane, it ought to be possible to find a third term which added to the above would represent a line in space. Argand and some others guessed that it was  $a + b\sqrt{-1} + c\sqrt{-1}\sqrt{-1}$  although this contradicts the truth established by Euler that  $\sqrt{-1}^{\sqrt{-1}} = e^{-\frac{1}{2}\pi}$ . De Morgan and many others worked hard at the problem, but nothing came of it until the problem was taken up by Hamilton. We now see the reason clearly: the symbol of double algebra denotes not a length and a direction; but a multiplier and *an angle*. In it the angles are confined to one plane; hence the next stage will be a *quadruple algebra*, when the axis of the plane is made variable. And this gives the answer to the first question; double algebra is nothing but analytical plane trigonometry, and this is the reason why it has been found to be the natural analysis for alternating currents. But De Morgan never got this far; he died with the belief that double algebra must remain as the full development of the conceptions of arithmetic, so far as those symbols are concerned which arithmetic

immediately suggests.”

When the study of mathematics revived at the University of Cambridge, so also did the study of logic. The moving spirit was Whewell, the Master of Trinity College, whose principal writings were a *History of the Inductive Sciences*, and *Philosophy of the Inductive Sciences*. Doubtless De Morgan was influenced in his logical investigations by Whewell; but other contemporaries of influence were Sir W. Hamilton of Edinburgh, and Professor Boole of Cork. De Morgan’s work on *Formal Logic*, published in 1847, is principally remarkable for his development of the numerically definite syllogism. The followers of Aristotle say and say truly that from two particular propositions such as *Some M’s are A’s*, and *Some M’s are B’s* nothing follows of necessity about the relation of the *A’s* and *B’s*. But they go further and say in order that any relation about the *A’s* and *B’s* may follow of necessity, the middle term must be taken universally in one of the premises. De Morgan pointed out that from *Most M’s are A’s* and *Most M’s are B’s* it follows of necessity that some *A’s* are *B’s* and he formulated the numerically definite syllogism which puts this principle in exact quantitative form. Suppose that the number of the *M’s* is  $m$ , of the *M’s* that are *A’s* is  $a$ , and of the *M’s* that are *B’s* is  $b$ ; then there are at least  $(a + b - m)$  *A’s* that are *B’s*. Suppose that the number of souls on board a steamer was 1000, that 500 were in the saloon, and 700 were lost; it follows of necessity, that at least  $700 + 500 - 1000$ , that is, 200, saloon passengers were lost. This single principle suffices to prove the validity of all the Aristotelian moods; it is therefore a fundamental principle in necessary reasoning.

Here then De Morgan had made a great advance by introducing quantification of the terms. At that time Sir W. Hamilton was teaching at Edinburgh a doctrine of the quantification of the predicate, and a correspondence sprang up. However, De Morgan soon perceived that Hamilton’s quantification was of a different character; that it meant for example, substituting the two forms *The whole of A is the whole of B*, and *The whole of A is a part of B* for the Aristotelian form *All A’s are B’s*. Philosophers generally have a large share of intolerance; they are too apt to think that they have got hold of the whole truth, and that everything outside of their system is error. Hamilton thought that he had placed the keystone in the Aristotelian arch, as he phrased it; although it must have been a curious arch which could stand 2000 years without a keystone. As a consequence he had no room for De Morgan’s innovations. He accused De Morgan of plagiarism, and the controversy raged for years in the columns of the *Athenæum*, and in the publications of the two writers.

The memoirs on logic which De Morgan contributed to the Transactions of the Cambridge Philosophical Society subsequent to the publication of his book on *Formal Logic* are by far the most important contributions which he made to the science, especially his fourth memoir, in which he begins work in the broad field of the *logic of relatives*. This is the true field for the logician of the twentieth century, in which work of the greatest importance is to be done towards improving language and facilitating thinking, processes which occur all the time in practical life. Identity and difference are the two relations which have been considered by the logician; but there are many others equally deserving of study, such as equality, equivalence, consanguinity, affinity, etc.

In the introduction to the *Budget of Paradoxes* De Morgan explains what he means by the word. “A great many individuals, ever since the rise of the mathematical method,

have, each for himself, attacked its direct and indirect consequences. I shall call each of these persons a paradoxer, and his system a paradox. I use the word in the old sense: a paradox is something which is apart from general opinion, either in subject matter, method, or conclusion. Many of the things brouht forward would now be called *crotchets*, which is the nearest word we have to old paradox. But there is this difference, that by calling a thing a crotchet we mean to speak lightly of it; which was not the necessary sense of paradox. Thus in the 16th century many spoke of the earth's motion as the paradox of Copernicus and held the ingenuity of that theory in very high esteem, and some I think who even inclined towards it. In the seventeenth century the depravation of meaning took place, in England at least."

How can the sound paradoxer be distinguished from the false paradoxer? De Morgan supplies the following test: "The manner in which a paradoxer will show himself, as to sense or nonsense, will not depend upon what he maintains, but upon whether he has or has not made a sufficient knowledge of what has been done by others, especially as to the mode of doing it, a preliminary to inventing knowledge for himself. . . . New knowledge, when to any purpose, must come by contemplation of old knowledge, in every matter which concerns thought; mechanical contrivance sometimes, not very often, escapes this rule. All the men who are now called discoverers, in every matter ruled by thought, have been men versed in the minds of their predecessors and learned in what had been before them. There is not one exception."

I remember that just before the American Association met at Indianapolis in 1890, the local newspapers heralded a great discovery which was to be laid before the assembled savants—a young man living somewhere in the country had squared the circle. While the meeting was in progress I observed a young man going about with a roll of paper in his hand. He spoke to me and complained that the paper containing his discovery had not been received. I asked him whether his object in presenting the paper was not to get it read, printed and published so that everyone might inform himself of the result; to all of which he assented readily. But, said I, many men have worked at this question, and their results have been tested fully, and they are printed for the benefit of anyone who can read; have you informed yourself of their results? To this there was no assent, but the sickly smile of the false paradoxer.

The *Budget* consists of a review of a large collection of paradoxical books which De Morgan had accumulated in his own library, partly by purchase at bookstands, partly from books sent to him for review, partly from books sent to him by the authors. He gives the following classification: squarers of the circle, trisectors of the angle, duplicators of the cube, constructors of perpetual motion, subverters of gravitation, stagnators of the earth, builders of the universe. You will still find specimens of all these classes in the New World and in the new century.

De Morgan gives his personal knowledge of paradoxers. "I suspect that I know more of the English class than any man in Britain. I never kept any reckoning. but I know that one year with another—and less of late years than in earlier time—I have talked to more than five in each year, giving more than a hundred and fifty specimens. Of this I am sure, that it is my own fault if they have not been a thousand. Nobody knows how they swarm, except those to whom they naturally resort. They are in all ranks' and occupations, of all ages and characters. They are very earnest people, and their purpose is *bona fide*, the dissemination of their paradoxes. A great many—the



mass, indeed—are illiterate, and a great many waste their means, and are in or approaching penury. These discoverers despise one another”

A paradoxer to whom De Morgan paid the compliment which Achilles paid Hector—to drag him round the walls again and again—was James Smith, a successful merchant of Liverpool. He found  $\pi = 3\frac{1}{8}$ . His mode of reasoning was a curious caricature of the *reductio ad absurdum* of Euclid. He said let  $\pi = 3\frac{1}{8}$ , and then showed that on that supposition, every other value of  $\pi$  must be absurd; consequently  $3\frac{1}{8}$  is the true value. The following is a specimen of De Morgan’s dragging round the walls of Troy: “Mr. Smith continues to write me long letters, to which he hints that I am to answer. In his last of 31 closely written sides of note paper, he informs me, with reference to my obstinate silence, that though I think myself and am thought by others to be a mathematical Goliath, I have resolved to play the mathematical snail, and keep within my shell. A mathematical *snail!* This cannot be the thing so called which regulates the striking of a clock; for it would mean that I am to make Mr. Smith sound the true time of day, which I would by no means undertake upon a clock that gains 19 seconds odd in every hour by false quadrature value of  $\pi$ . But he ventures to tell me that pebbles from the sling of simple truth and common sense will ultimately crack my shell, and put me *hors de combat*. The confusion of images is amusing: Goliath turning himself into a snail to avoid  $\pi = 3\frac{1}{8}$  and James Smith, Esq., of the Mersey Dock Board: and put *hors de combat* by pebbles from a sling. If Goliath had crept into a snail shell, David would have cracked the Philistine with his foot. There is something like modesty in the implication that the crack-shell pebble has not yet taken effect. It might have been thought that the slinger would by this time have been singing—And thrice [and one-eighth] I routed all my foes, And thrice [and one-eighth] I slew the slain.”

In the region of pure mathematics De Morgan could detect easily the false from the true paradox; but he was not so proficient in the field of physics. His father-in-law was a paradoxer, and his wife a paradoxer; and in the opinion of the physical philosophers De Morgan himself scarcely escaped. His wife wrote a book describing the phenomena of spiritualism, table-rapping, table-turning, etc.; and De Morgan wrote a preface in which he said that he knew some of the asserted facts, believed others on testimony, but did not pretend to know *whether* they were caused by spirits, or had some unknown and unimagined origin. From this alternative he left out ordinary material causes. Faraday delivered a lecture on *Spiritualism*, in which he laid it down that in the investigation we ought to set out with the idea of what is physically possible, or impossible; De Morgan could not understand this.

From A Macfarlane, *Lectures on Ten British Mathematicians of the Nineteenth Century*, New York: Wiley and London: Chapman and Hall 1916, pp. 19–33.